PHYSICAL CONDITIONS IN REGIONS OF STAR FORMATION

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Abstract  The physical conditions in molecular clouds control the nature and rate of star formation, with consequences for planet formation and galaxy evolution. The focus of this review is on the conditions that characterize regions of star formation in our Galaxy. A review of the tools and tracers for probing physical conditions includes summaries of generally applicable results. Further discussion distinguishes between the formation of low-mass stars in relative isolation and formation in a clustered environment. Evolutionary scenarios and theoretical predictions are more developed for isolated star formation, and observational tests are beginning to interact strongly with the theory. Observers have identified dense cores collapsing to form individual stars or binaries, and analysis of some of these cores support theoretical models of collapse. Stars of both low and high mass form in clustered environments, but massive stars form almost exclusively in clusters. The theoretical understanding of such regions is considerably less developed, but observations are providing the ground rules within which theory must operate. The richest and most massive star clusters form in massive, dense, turbulent cores, which provide models for star formation in other galaxies.

1. INTRODUCTION

Long after their parent spiral galaxies have formed, stars continue to form by repeated condensation from the interstellar medium. In the process, parts of the interstellar medium pass through a cool, relatively dense phase with a great deal of complexity—molecular clouds. While both the diffuse interstellar medium and stars can be supported by thermal pressure, most molecular clouds cannot be thermally supported (Goldreich & Kwan 1974). Simple consideration would suggest that molecular clouds would be a very transient phase in the conversion of diffuse gas to stars, but in fact they persist much longer than expected. During this extended life, they produce an intricate physical and chemical system that provides the substrate for the formation of planets and life, as well as stars. Comparison of cloud masses to the total mass of stars that they produce indicates that most of the matter in a molecular cloud is sterile; stars form only in a small fraction of the mass of the cloud (Leisawitz et al 1989).
The physical conditions in the bulk of a molecular cloud provide the key to understanding why molecular clouds form an essentially metastable state along the path from diffuse gas to stars. Most of the mass of most molecular clouds in our Galaxy is contained in regions of modest extinction, allowing photons from the interstellar radiation field to maintain sufficient ionization for magnetic fields to resist collapse (McKee 1989); most of the molecular gas is, in fact, in a photon-dominated region (PDR) (Hollenbach & Tielens 1997). In addition, most molecular gas has supersonic turbulence (Zuckerman & Evans 1974). The persistence of such turbulence over the inferred lifetimes of clouds in the face of rapid damping mechanisms (Goldreich & Kwan 1974) suggests constant replenishment, most likely in a process of self-regulated star formation (Norman & Silk 1980, Bertoldi & McKee 1996), because star formation is accompanied by energetic outflows, jets, and winds (Bachiller 1996).

For this review, the focus is on the physical conditions in regions that are forming stars and likely precursors of such regions. Although gravitational collapse explains the formation of stars, the details of how it happens depend critically on the physical conditions in the star-forming region. The details determine the mass of the resulting star and the amount of mass that winds up in a disk around the star, in turn controlling the possibilities for planet formation. The physical conditions also control the chemical conditions. With the recognition that much interstellar chemistry is preserved in comets (Crovisier 1999, van Dishoeck & Blake 1998) and that interstellar chemistry may also affect planet formation and the possibilities for life (e.g. Pendleton 1997, Pendleton & Tielens 1997, Chyba & Sagan 1992), the knowledge of physical conditions in star-forming regions has taken on additional significance.

Thinking more globally, different physical conditions in different regions determine whether a few lightly clustered stars form (the isolated mode) or a tight grouping of stars forms (the clustered mode) (Lada 1992, Lada et al 1993). The star formation rates per unit mass of molecular gas vary by a factor of $>10^2$ in clouds within our own Galaxy (Evans 1991, Mead et al 1990), and starburst galaxies achieve even higher rates than are seen anywhere in our Galaxy (e.g. Sanders et al 1991). Ultimately, a description of galaxy formation must incorporate an understanding of how star formation depends on physical conditions, gleaned from careful study of our Galaxy and nearby galaxies.

Within the space limitations of this review, it is not possible to address all of the issues raised by the preceding overview. I generally avoid topics that have been recently reviewed, such as circumstellar disks (Sargent 1996, Papaloizou & Lin 1995, Lin & Papaloizou 1996, Bodenheimer 1995), as well as bipolar outflows (Bachiller 1996) and dense PDRs (Hollenbach & Tielens 1997). I also discuss the sterile parts of molecular clouds only as relevant to the process that leads some parts of the cloud to be suitable for star formation. While the chemistry and physics of star-forming regions are coupled, chemistry has been recently reviewed (van Dishoeck & Blake 1998). Astronomical masers are being concurrently reviewed.
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(Menten, in preparation); as with HII regions, they are discussed only as signposts for regions of star formation.

I will focus on star formation in our Galaxy. Nearby regions of isolated, low-mass star formation will receive considerable attention (Section 4) because we have made the most progress in studying them. Their conditions will be compared with those in regions forming clusters of stars, including massive stars (Section 5). These regions of clustered star formation are poorly understood, but they probably form the majority of stars in our Galaxy (Elmegreen 1985), and they are the regions relevant for comparisons to other galaxies.

Even with such a restricted topic, the literature is vast. I make no attempt at completeness in referencing. On relatively noncontroversial topics, I tend to give an early reference and a recent review; for more unsettled topics, more references, with different points of view, are given. Recent or upcoming publications with significant overlap include Hartmann (1998), Lada & Kylafis (1999), and Mannings et al (2000).

2. PHYSICAL CONDITIONS

The motivation for studying physical conditions can be found in a few simple theoretical considerations. Our goal is to know when and how molecular gas collapses to form stars. In the simplest situation—a cloud with only thermal support—collapse should occur if the mass exceeds the Jeans (1928) mass,

$$M_J = \left( \frac{\pi k T_K}{\mu m_H G} \right)^{1.5} \rho^{0.5} = 18 M_\odot T_k^{1.5} n^{-0.5},$$

(1)

where $T_K$ is the kinetic temperature (kelvins), $\rho$ is the mass density (g cm$^{-3}$), and $n$ is the total particle density (cm$^{-3}$). In a molecular cloud, H nuclei are almost exclusively in H$_2$ molecules, and $n \sim n$(H$_2$) + $n$(He). Then $\rho = \mu_n m_H n$, where $m_H$ is the mass of a hydrogen atom and $\mu_n$ is the mean mass per particle (2.29 in a fully molecular cloud with 25% by mass helium). Discrepancies between coefficients in the equations presented here and those in other references usually are traceable to a different definition of $n$. In the absence of pressure support, collapse will occur in a free-fall time (Spitzer 1978),

$$t_{ff} = \left( \frac{3\pi}{32G\rho} \right)^{0.5} = 3.4 \times 10^7 n^{-0.5} \text{ years.}$$

(2)

If $T_K = 10$ K and $n \geq 50$ cm$^{-3}$, typical conditions in the sterile regions (e.g. Blitz 1993), $M_J \leq 80 M_\odot$, and $t_{ff} \leq 5 \times 10^6$ years. Our Galaxy contains about $1-3 \times 10^8 M_\odot$ of molecular gas (Bronfman et al 1988, Clemens et al 1988, Combes 1991). The majority of this gas is probably contained in clouds with $M > 10^4 M_\odot$. 
It would be highly unstable on these grounds, and free-fall collapse would lead to a star formation rate, \( M_\ast \geq 200 \, M_\odot \, \text{year}^{-1} \), far in excess of the recent galactic average of \( 3 \, M_\odot \, \text{year}^{-1} \) (Scalo 1986). This argument, first made by Zuckerman & Palmer (1974), shows that most clouds cannot be collapsing at free fall (see also Zuckerman & Evans 1974). Together with evidence of cloud lifetimes of about \( 4 \times 10^7 \) years (Bash et al 1977, Leisawitz et al 1989), this discrepancy motivates an examination of other support mechanisms.

Two possibilities have been considered, magnetic fields and turbulence. Calculations of the stability of magnetized clouds (Mestel & Spitzer 1956, Mestel 1965) led to the concept of a magnetic critical mass \( (M_B) \). For highly flattened clouds (Li & Shu 1996),

\[
M_B = (2\pi)^{-1} G^{-0.5} \Phi,
\]

where \( \Phi \) is the magnetic flux threading the cloud,

\[
\Phi \equiv \int B \, da.
\]

Numerical calculations (Mouschovias & Spitzer 1976) indicate a similar coefficient (0.13). If turbulence can be thought of as causing pressure, it may be able to stabilize clouds on large scales (e.g. Bonazzola et al 1987). It is not at all clear that turbulence can be treated so simply. In both cases, the cloud can only be metastable. Gas can move along field lines, and ambipolar diffusion will allow neutral gas to move across field lines with a timescale of \( (\text{McKee et al 1993}) \)

\[
t_{AD} = \frac{3}{4\pi G \rho \tau_{ni}} \simeq 7.3 \times 10^{13} x_e \, \text{years},
\]

where \( \tau_{ni} \) is the ion-neutral collision time. The ionization fraction \( (x_e) \) depends on ionization by photons and cosmic rays, balanced by recombination. It thus depends on the abundances of other species \( [X(x) \equiv n(x)/n] \).

These two suggested mechanisms of cloud support (magnetic and turbulent) are not entirely compatible because turbulence should tangle the magnetic field (compare the reviews by Mouschovias 1999 and McKee 1999). A happy marriage between magnetic fields and turbulence was long hoped for; Arons & Max (1975) suggested that magnetic fields would slow the decay of turbulence if the turbulence was sub-Alfvénic. Simulations of MHD turbulence in systems with high degrees of symmetry supported this suggestion and indicated that the pressure from magnetic waves could stabilize clouds (Gammie & Ostriker 1996). However, more recent three-dimensional simulations indicate that MHD turbulence decays rapidly and that replenishment is still needed (Mac Low et al 1998, Stone et al 1999). The usual suggestion is that outflows generate turbulence, but Zweibel (1998) has suggested that an instability induced by ambipolar diffusion may convert magnetic energy into turbulence. Finally, the issue of supporting clouds assumes a certain stability and cloud integrity that may be misleading in a dynamic interstellar medium (e.g.,...

With this brief and simplistic review of the issues of cloud stability and evolution, we have motivated the study of the basic physical conditions:

$$T_K, n, \vec{v}, \vec{B}, X.$$  

(6)

All of these are local variables; in principle, they can have different values at each point ($\vec{r}$) in space and can vary with time ($t$). In practice, we usually can measure only one component of vector quantities, integrated through the cloud. For example, we measure only line-of-sight velocities, usually characterized by the line width ($\Delta v$) or higher moments, and the line-of-sight magnetic field ($B_z$) through the Zeeman effect, or the projected direction (but not the strength) of the field in the plane of the sky ($B_\perp$) by polarization studies. In addition, our observations always average over finite regions, so we attempt to simplify the dependence on $\vec{r}$ by assumptions or models of cloud structure. In Section 3, I describe the methods used to probe these quantities and some overall results. Abundances have been reviewed recently (van Dishoeck & Blake 1998), so only relevant results will be mentioned, most notably the ionization fraction $x_e$.

In addition to the local variables, quantities that explicitly integrate over one or more dimensions are often measured. Foremost is the column density,

$$N \equiv \int ndl.$$  

(7)

The extinction or optical depth of dust at some wavelength is a common surrogate measure of $N$. If the column density is integrated over an area, one measure of the cloud mass within that area is obtained:

$$M_N \equiv \int N \, da.$$  

(8)

Another commonly used measure of mass is obtained by simplification of the virial theorem. If external pressure and magnetic fields are ignored,

$$M_V = C_v G^{-1} R \Delta v^2 = 210 M_\odot C_v R (pc) [\Delta v (\text{km s}^{-1})]^2,$$  

(9)

where $R$ is the radius of the region, $\Delta v$ is the FWHM line width, and the constant ($C_v$) depends on geometry and cloud structure, but is of order unity (e.g. McKee & Zweibel 1992, Bertoldi & McKee 1992). A third mass estimate can be obtained by integrating the density over the volume,

$$M_n \equiv \int ndv.$$  

(10)

$M_n$ is commonly used to estimate $f_v$, the volume-filling factor of gas at density $n$, by dividing $M_n$ by another mass estimate, typically $M_V$. Of the three methods of mass determination, the virial mass is the least sensitive to uncertainties in distance and size, but care must be taken to exclude unbound motions, such as outflows.
Parallel to the physical conditions in the gas, the dust can be characterized by a set of conditions:

\[ T_D, n_D, \kappa(\nu), \]  

(11)

where \( T_D \) is the dust temperature, \( n_D \) is the density of dust grains, and \( \kappa(\nu) \) is the opacity at a given frequency, \( \nu \). If we look in more detail, grains have a range of sizes (Mathis et al 1977) and compositions. For smaller grains, \( T_D \) is a function of grain size. Thus, we would have to characterize the temperature distribution as a function of size, the composition of grains, both core and mantle, and many more optical constants to capture the full range of grain properties. For our purposes, \( T_D \) and \( \kappa(\nu) \) are the most important properties, because \( T_D \) affects gas energetics and \( T_D \) and \( \kappa(\nu) \) control the observed continuum emission of molecular clouds. The detailed nature of the dust grains may come into play in several situations, but the primary observational manifestation of the dust is its ability to absorb and emit radiation. For this review, a host of details can be ignored. The optical depth is set by

\[ \tau_D(\nu) = \kappa(\nu)N, \]  

(12)

where it is convenient to define \( \kappa(\nu) \) so that \( N \) is the gas column density rather than the dust column density. Away from resonances, the opacity is usually approximated by \( \kappa(\nu) \propto \nu^\beta \).

3. PROBES OF PHYSICAL CONDITIONS

The most fundamental fact about molecular clouds is that most of their contents are invisible. Neither the H\(_2\) nor the He in the bulk of the clouds is excited sufficiently to emit. Although fluorescent emission from H\(_2\) can be mapped over the face of clouds (Luhman & Jaffe 1996), the UV radiation needed to excite this emission does not penetrate the bulk of the cloud. In shocked regions, H\(_2\) emits rovibrational lines that are useful probes of \( T_K \) and \( \vec{v}(\vec{r}) \) (e.g. Draine & McKee 1993). Absorption by H\(_2\) of background stars is also difficult: the dust in molecular clouds obnubilates the UV that would reveal electronic transitions; the rotational transitions are so weak that only huge \( N \) would produce absorption, and the dust again obnubilates background sources; only the vibrational transitions in the near-infrared have been seen in absorption in only a few molecular clouds (Lacy et al 1994). Gamma rays resulting from cosmic-ray interactions with atomic nuclei do probe all the material in molecular clouds (Bloemen 1989, Strong et al 1994). So far, gamma-ray studies have suffered from low spatial resolution and uncertainties in the cosmic ray flux; they have been used mostly to check consistency with other tracers on large scales.

In the following subsections, I discuss probes of different physical quantities, including some general results, concluding with a discussion of the observational and analytical tools. Genzel (1992) has presented a detailed discussion of probes of physical conditions.
3.1 Tracers of Column Density, Size, and Mass

Given the reticence of the bulk of the H$_2$, essentially all probes of physical conditions rely on trace constituents, such as dust particles and molecules other than H$_2$. Dust particles (Mathis 1990, Pendleton & Tielens 1997) attenuate light at short wavelengths (UV to near infrared) and emit at longer wavelengths (far infrared to millimeter). Assuming that the ratio of dust extinction at a fixed wavelength to gas column density is constant, one can use extinction to map $N$ in molecular clouds, and early work at visible wavelengths revealed locations and sizes of many molecular clouds before they were known to contain molecules (Barnard 1927, Bok & Reilly 1947, Lynds 1962). There have been more recent surveys for small clouds (Clemens & Barvainis 1988) and for clouds at high latitude (Blitz et al 1984). More recently, near-infrared surveys have been used to probe much more deeply; in particular, the $H - K$ color excess can trace $N$ to an equivalent visual extinction, $A_V \sim 30$ mag (Lada et al 1994, Alves et al 1998). This method provides many pencil beam measurements through a cloud toward background stars. The very high-resolution but very undersampled data require careful analysis but can reveal information on mass, large-scale structure in $N$, and unresolved structure (Alves et al 1998). Padoan et al (1997) interpret the data of Lada et al (1994) in terms of a lognormal distribution of density, but Lada et al (1999) show that a cylinder with a density gradient $n(r) \propto r^{-2}$ also matches the observations.

Continuum emission from dust at long wavelengths is complementary to absorption studies (e.g. Chandler & Sargent 1997). Because the dust opacity decreases with increasing wavelength [$\kappa(\nu) \propto \nu^\beta$, with $\beta \sim 1-2$], emission at long wavelengths can trace large column densities and provide independent mass estimates (Hildebrand 1983). The data can be fully sampled and have reasonably high resolution. The dust emission depends on the dust temperature ($T_D$), linearly if the observations are firmly in the Rayleigh-Jeans limit, but exponentially on the Wien side of the blackbody curve. Observations on both sides of the emission peak can constrain $T_D$. Opacities have been calculated for a variety of scenarios including grain mantle formation and collisional concrescence (e.g. Ossenkopf & Henning 1994). For grain sizes much less than the wavelength, $\beta \sim 2$ is expected from simple grain models, but observations of dense regions often indicate lower values. By observing at a sufficiently long wavelength, one can trace $N$ to very high values. Recent results indicate that $\tau_D(1.2 \text{ mm}) = 1$ only for $A_V \sim 4 \times 10^4$ mag (Kramer et al 1998a) in the less dense regions of molecular clouds. In dense regions, there is considerable evidence for increased grain opacity at long wavelengths (Zhou et al 1990, van der Tak et al 1999), suggesting grain growth through collisional concrescence in addition to the formation of icy mantles. Further growth of grains in disks is also likely (Chandler & Sargent 1997).

The other choice is to use a trace constituent of the gas, typically molecules that emit in their rotational transitions at millimeter or submillimeter wavelengths. By using the appropriate transitions of the appropriate molecule, one can tune the probe to study the physical quantity of interest and the target region along the line
of sight. This technique was first used with OH (Barrett et al. 1964), and it has been pursued intensively in the 30 years since the discovery of polyatomic interstellar molecules (Cheung et al. 1968, van Dishoeck & Blake 1998).

The most abundant molecule after H$_2$ is carbon monoxide; the main isotopomer ($^{12}$C$^{16}$O) is usually written simply as CO. It is the most common tracer of molecular gas. On the largest scales, CO correlates well with the gamma-ray data (Strong et al. 1994), suggesting that the overall mass of a cloud can be measured even when the line is quite opaque. This stroke of good fortune can be understood if the clouds are clumpy and macroturbulent, with little radiative coupling between clumps (Wolfire et al. 1993); in this case, the CO luminosity is proportional to the number of clumps, hence total mass. Most of the mass estimates for the larger clouds and for the total molecular mass in the Galaxy and in other galaxies are in fact based on CO. On smaller scales and in regions of high column density, CO fails to trace column density, and progressively rarer isotopomers are used to trace progressively higher values of $N$. Dickman (1978) established a strong correlation of visual extinction $A_V$ with $^{13}$CO emission for $1.5 \leq A_V \leq 5$. Subsequent studies have used C$^{18}$O and C$^{17}$O to trace still higher $N$ (Frerking et al. 1982). These rarer isotopomers will not trace the outer parts of the cloud, where photodissociation affects them more strongly than the common isotopomers, but we are concerned with the more opaque regions in this review.

When comparing $N$ measured by dust emission with $N$ traced by CO isotopomers, it is important to correct for the fact that emission from low-$J$ transitions of optically thin isotopomers of CO decreases with $T_K$, whereas dust emission increases with $T_D$ (Jaffe et al. 1984). Observations of many transitions can avoid this problem but are rarely done. To convert $N$(CO) to $N$ requires knowledge of the abundance, $X$(CO). The only direct measure gave $X$(CO) = $2.7 \times 10^{-4}$ (Lacy et al. 1994), three times greater than inferred from indirect means (e.g. Frerking et al. 1982). Clearly, this area needs increased attention, but at least a factor of 3 uncertainty must be admitted. Studies of some particularly opaque regions in molecular clouds indicate severe depletion (Kuiper et al. 1996, Bergin & Langer 1997), raising the concern that even the rare CO isotopomers may fail to trace $N$. Indeed, Alves et al. (1999) find that C$^{18}$O fails to trace column density above $A_V = 10$ in some regions, and Kramer et al. (1999) argue that this failure is best explained by depletion of C$^{18}$O.

Sizes of clouds, characterized by either a radius ($R$) or diameter ($l$), are measured by mapping the cloud in a particular tracer; for nonspherical clouds, these are often the geometric mean of two dimensions, and the aspect ratio ($a/b$) characterizes the ratio of long and short axes. The size along the line of sight (depth) can be constrained only by making geometrical assumptions (usually of a spherical or cylindrical cloud). One possible probe of the depth is H$_3^+$, which is unusual in having a calculable, constant density in molecular clouds. Thus, a measurement of $N$(H$_3^+$) can yield a measure of cloud depth (Geballe & Oka 1986).

With a measure of size and a measure of column density, the mass ($M_N$) may be estimated (Equation 8); with a size and a line width ($\Delta v$), the virial mass ($M_V$) can
be estimated (Equation 9). On the largest scales, the mass is often estimated from integrating the CO emission over the cloud and using an empirical relation between mass and the CO luminosity, \( L(\text{CO}) \). The mass distribution has been estimated for both clouds and clumps within clouds, primarily from CO, \(^{13}\text{CO}\), or \(^{18}\text{O}\), using a variety of techniques to define clumps and estimate masses (Blitz 1993, Kramer et al 1998b, Heyer & Terebey 1998, Heithausen et al 1998). These studies have covered a wide range of masses, with Kramer et al extending the range down to \( M = 10^{-4} \, M_\odot \). The result is fairly well agreed on: \( dN(M) \propto M^{-\alpha} \, dM \), with \( 1.5 \leq \alpha \leq 1.9 \). Elmegreen & Falgarone (1996) have argued that the mass spectrum is a result of the fractal nature of the interstellar gas, with a fractal dimension \( D = 2.3 \pm 0.3 \). There is disagreement over whether clouds are truly fractal or have a preferred scale (Blitz & Williams 1997). On one hand, the latter authors suggest a scale of 0.25–0.5 pc in Taurus based on \(^{13}\text{CO}\). On the other hand, Falgarone et al (1998), analyzing an extensive data set, find evidence for continued structure down to 200 AU in gas that is not forming stars. The initial mass function (IMF) of stars is steeper than the cloud mass distribution for \( M_\ast > 1 \, M_\odot \) but is flatter than the cloud mass function for \( M_\ast < 1 \, M_\odot \) (e.g. Scalo 1998). Understanding the origin of the differences is a major issue (see Williams et al 2000, Meyer et al 2000).

### 3.2 Probes of Temperature and Density

The abundances of other molecules are so poorly constrained that CO isotopomers and dust are used almost exclusively to constrain \( N \) and \( M_\ast \). Of what use are the >100 other molecules? Although many are of interest only for astrochemistry, some are very useful probes of physical conditions like \( T_K \), \( n \), \( v \), \( B_z \), and \( x_e \).

Density (\( n \)) and gas temperature (\( T_K \)) are both measured by determining the populations in molecular energy levels and comparing the results to calculations of molecular excitation. A useful concept is the excitation temperature (\( T_{ex} \)) of a pair of levels, defined to be the temperature that gives the actual ratio of populations in those levels, when substituted into the Boltzmann equation. In general, collisions and radiative processes compete to establish level populations; when lines are optically thick, trapping of line photons enhances the effects of collisions. For some levels in some molecules, radiative rates are unusually low, collisions dominate, \( T_{ex} = T_K \), and observational determination of these “thermalized” level populations yields \( T_K \). Unthermalized level populations depend on both \( n \) and \( T_K \); with a knowledge of \( T_K \), observational determination of these populations yields \( n \), although trapping usually needs to be accounted for. While molecular excitation probes the local \( n \) and \( T_K \) in principle, the observations themselves always involve some average over the finite beam and along the line of sight. Consequently, a model of the cloud is needed to interpret the observations. The simplest model is of course a homogeneous cloud, and most early work adopted this model, either explicitly or implicitly.

Tracers of temperature include CO, with its unusually low dipole moment, and molecules in which transitions between certain levels are forbidden by selection
rules. The latter include different $K$ ladders of symmetric tops like $\text{NH}_3$, $\text{CH}_3\text{CN}$, etc. (Ho & Townes 1983, Loren & Mundy 1984). Different $K_{-1}$ ladders in $\text{H}_2\text{CO}$ also probe $T_K$ in dense, warm regions (Mangum & Wootten 1993). A useful feature of CO is that its low-$J$ transitions are both opaque and thermalized in most parts of molecular clouds. In this case, observations of a single line provide the temperature, after correction for the cosmic background radiation and departures from the Rayleigh-Jeans approximation (Penzias et al 1972, Evans 1980). Early work on CO (Dickman 1975) and $\text{NH}_3$ (Martin & Barrett 1978) established that $T_K \simeq 10$ K far from regions of star formation and that sites of massive star formation are marked by elevated $T_K$, revealed by peaks in maps of CO (e.g. Blair et al 1975).

The value of $T_K$ far from local heating sources can be understood by balancing cosmic-ray heating and molecular cooling (Goldsmith & Langer 1978), while elevated values of $T_K$ in star-forming regions have a more intricate explanation. Stellar photons, even when degraded to the infrared, do not couple well to molecular gas, so the heating goes via the dust. The dust is heated by photons, and the gas is heated by collisions with the dust (Goldreich & Kwan 1974); above a density of about $10^4$ cm$^{-3}$, $T_K$ becomes well coupled to $T_D$ (Takahashi et al 1983). Observational comparison of $T_K$ to $T_D$, determined from far-infrared observations, supports this picture (e.g. Evans et al 1977, Wu & Evans 1989).

In regions where photons in the range of 6 to 13.6 eV impinge directly on molecular material, photoelectrons ejected from dust grains can heat the gas very effectively, and $T_K$ may exceed $T_D$. These PDRs (Hollenbach & Tielens 1997) form the surfaces of all clouds, but the regions affected by these photons are limited by dust extinction to about $A_V \sim 8$ mag (McKee 1989). However, the CO lines often do form in the PDR regions, raising the question of why they indicate that $T_K \sim 10$ K. Wolfire et al (1993) explain that the optical depth in the lower-$J$ levels usually observed reaches unity at a place where the $T_K$ and $n$ combine to produce an excitation temperature ($T_{\text{ex}}$) of about 10 K. Thus, the agreement of $T_K$ derived from CO with the predictions of energetics calculations for cosmic-ray heating may be fortuitous. The $T_K$ derived from $\text{NH}_3$ refer to more opaque regions and are more relevant to cosmic-ray heating. Finally, in localized regions, shocks can heat the gas to very high $T_K$; values of 2000 K are observed in $\text{H}_2$ rovibrational emission lines (Beckwith et al 1978). It is clear that characterizing clouds by a single $T_K$, which is often done for simplicity, obscures a great deal of complexity.

Density determination requires observations of several transitions that are not in local thermodynamic equilibrium (LTE). Then the ratio of populations, or equivalently $T_{\text{ex}}$, can be used to constrain density. A useful concept is the critical density for a transition from level $j$ to level $k$,

$$n_c(jk) = A_{jk} \gamma_{jk},$$

where $A_{jk}$ is the Einstein A coefficient and $n\gamma_{jk}$ is the collisional deexcitation rate per molecule in level $j$. In general, both $\text{H}_2$ and He are effective collision partners,
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<th>Molecule</th>
<th>Transition</th>
<th>ν (GHz)</th>
<th>$E_{up}$ (K)</th>
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<th>$n_e (10^5)$ (cm$^{-3}$)</th>
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<td>$6.2 \times 10^7$</td>
<td>$1.7 \times 10^6$</td>
</tr>
<tr>
<td>HCO$^+$</td>
<td>$J = 1 \rightarrow 0$</td>
<td>89.2</td>
<td>4.3</td>
<td>$1.7 \times 10^5$</td>
<td>$2.4 \times 10^3$</td>
<td>$1.9 \times 10^5$</td>
<td>$5.6 \times 10^2$</td>
</tr>
<tr>
<td>HCO$^+$</td>
<td>$J = 3 \rightarrow 2$</td>
<td>267.6</td>
<td>26</td>
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<td>$6.3 \times 10^4$</td>
<td>$3.3 \times 10^6$</td>
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<td>$J = 4 \rightarrow 3$</td>
<td>356.7</td>
<td>43</td>
<td>$9.7 \times 10^6$</td>
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<td>6.8</td>
<td>$1.1 \times 10^8$</td>
<td>$6.0 \times 10^6$</td>
<td>$1.6 \times 10^8$</td>
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<td>211.2</td>
<td>17</td>
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<td>$5_{15} \rightarrow 4_{14}$</td>
<td>351.8</td>
<td>47</td>
<td>$2.6 \times 10^9$</td>
<td>...</td>
<td>$2.5 \times 10^7$</td>
<td>$2.0 \times 10^5$</td>
</tr>
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<td>(1,1)inv</td>
<td>23.7</td>
<td>1.1</td>
<td>$1.8 \times 10^3$</td>
<td>$1.2 \times 10^3$</td>
<td>$2.1 \times 10^3$</td>
<td>$7.0 \times 10^2$</td>
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<td>42</td>
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<td>$3.6 \times 10^4$</td>
<td>$2.1 \times 10^3$</td>
<td>$4.3 \times 10^2$</td>
</tr>
</tbody>
</table>

... means no value; inv means inversion transition.

with comparable collision rates, so that excitation techniques measure the total density of collision partners, $n \simeq n(H_2) + n(He)$. In some regions of high $x_e$, collisions with electrons may also be significant. Detection of a particular transition is often taken to imply that $n \geq n_c(jk)$, but this statement is too simplistic. Lines can be seen over a wide range of $n$, depending on observational sensitivity, the frequency of the line, and the optical depth (e.g. Evans 1989). Observing high frequency transitions, multilevel excitation effects, and trapping all tend to lower the effective density needed to detect a line. Table 1 contains information for some commonly observed lines, including the frequency, energy in K above the effective ground state [$E_{up}(K)$], and the critical densities at $T_K = 10$ K and 100 K. For comparison, the Table also has $n_{eff}$, the density needed to produce a line of 1 K, easily observable in most cases. The values of $n_{eff}$ were calculated with a large velocity gradient (LVG) code (Section 3.5) to account for trapping, assuming log($N/\Delta v) = 13.5$ for all species but NH$_3$, for which log($N/\Delta v) = 15$ was used. $N/\Delta v$ has units of cm$^{-2}$ (km s$^{-1}$)$^{-1}$. These column densities are typical and produce modest optical depths. Note that $n_{eff}$ can be as much as a factor of
1000 less than the critical density, especially for high excitation lines and high $T_K$.
Clearly, the critical density should be used as a guideline only; more sophisticated analysis is necessary to infer densities.

Assuming that we have knowledge of $T_K$, at least two transitions with different $n_c(jk)$ are needed to determine both $n$ and the line optical depth, $\tau_{jk} \propto N_k/\Delta v$, which determines the amount of trapping, and more transitions are desirable. Because $A_{J,J-1} \propto J^3$, where $J$ is the quantum number for total angular momentum, observing many transitions up a rotational energy ladder provides a wide range of $n_c(jk)$. Linear molecules, like HCN and HCO$^+$, have been used in this way, but higher levels often occur at wavelengths with poor atmospheric transmission. Relatively heavy species, like CS, have many accessible transitions, and up to five transitions ranging up to $J = 10$ have been used to constrain density (e.g. Carr et al 1995, van der Tak et al 1999). More complex species provide more accessible energy levels; transitions within a single $K_{-1}$ ladder of H$_2$CO provide a valuable density probe (Mangum & Wootten 1993). Transitions of H$_2$CO with $\Delta J = 0$ are accessible to large arrays operating at centimeter wavelengths (e.g. Evans et al 1987). The lowest few of these H$_2$CO transitions have the interesting property of absorbing the cosmic background radiation (Palmer et al 1969), $T_\text{ex}$ being cooled by collisional pumping (Towner & Cheung 1969).

Application of these techniques to the homogeneous cloud model generally produces estimates of density exceeding $10^4$ cm$^{-3}$ in regions forming stars, while the sterile regions of the cloud are thought to have typical $n \sim 10^2 - 10^3$ cm$^{-3}$, although these are less well constrained. Theoretical simulations of turbulence have predicted lognormal (Vázquez-Semadini 1994) or power-law (Scalo et al 1998) probability density functions. Studies of multiple transitions of different molecules with a wide range of critical densities often reveal evidence for density inhomogeneities; in particular, pairs of transitions with higher critical densities tend to indicate higher densities (e.g. Evans 1980, Plume et al 1997). Both density gradients and clumpy structure have been invoked to explain these results (see Sections 4 and 5 for detailed discussion). Because lines with high $n_c(jk)$ are excited primarily at higher $n$, one can avoid to some extent the averaging over the line of sight by tuning the probe.

### 3.3 Kinematics

In principle, information on $\vec{v}(\vec{r})$ is contained in maps of the line profile over the cloud. In practice, this message has been difficult to decode. Only motions along the line of sight produce Doppler shifts, and the line profiles average over the beam and along the line of sight. Maps of the line center velocity generally indicate that the typical cloud is experiencing neither overall collapse (Zuckerman & Evans 1974) nor rapid rotation (Arquilla & Goldsmith 1986, Goodman et al 1993). Instead, most clouds appear to have velocity fields dominated by turbulence, because the line widths are usually much greater than expected from thermal broadening. Although such turbulence can explain the breadth of the lines, the line profile is
not easily matched. Even a homogeneous cloud will tend to develop an excitation gradient in unthermalized lines because of trapping, and gradients in $T_k$ or $n$ toward embedded sources should exacerbate this tendency. Simple microturbulent models with decreasing $T_e(r)$ predict that self-reversed line profiles should be seen more commonly than they are. Models with many small clumps and macroturbulence have had some success in avoiding self-reversed line profiles (Martin et al 1984, Wolfire et al 1993, Falgarone et al 1994, Park & Hong 1995).

The average line widths of clouds are larger for larger clouds, the line width-size relation: $\Delta v \propto R^{\gamma}$ (Larson 1981). For clouds with the same $N$, the virial theorem would predict $\gamma = 0.5$, consistent with the results of many studies of clouds as a whole (e.g. Solomon et al 1987). Myers (1985) summarized the different relations and distinguished between those comparing clouds as a whole and those studying trends within a single cloud. The status of line width-size relations within clouds, particularly in star-forming regions, will be discussed in later sections.

### 3.4 Magnetic Field and Ionization

The magnetic field strength and direction are important but difficult to measure. Heiles et al (1993) review the observations, and McKee et al (1993) review theoretical issues. The only useful measure of the strength is the Zeeman effect, which probes the line-of-sight field $B_z$. Observations of HI can provide some useful probes of $B_z$ in PDRs (e.g. Brogan et al 1999), but cannot probe the bulk of molecular gas. Molecules suitable for Zeeman effect measurements have unpaired electrons, and their resulting reactivity tends to decrease their abundance in the denser regions (e.g. Sternberg et al 1997). Almost all work has been done with OH, along with some work with CN (Crutcher et al 1996), but future prospects include CCS and excited states of OH and CH (Crutcher 1998). Measurements of $B_z$ have been made with thermal emission or absorption by OH (e.g. Crutcher et al 1993), mostly probing regions with $n \sim 10^3$ cm$^{-3}$, where $B_z \simeq 20$ $\mu$G or with OH maser emission, probing much denser gas, but with less certain conditions. As reviewed by Crutcher (1999a), the results for 14 clouds of widely varying mass with good Zeeman detections indicate that $M_B$ is usually within a factor of 2 of the cloud mass. Given uncertainties, this result suggests that clouds with measured $B_z$ lie close to the critical-subcritical boundary (Shu et al 1999). The observations can be fit with $B \propto n^{0.47}$, remarkably consistent with predictions of ambipolar-diffusion calculations (e.g. Fiedler & Mouschovias 1993). However, if turbulent motions in clouds are constrained to be comparable to the Alfvén velocity, $v_A \propto Bn^{-0.5}$, this result is also expected (Myers & Goodman 1988, Bertoldi & McKee 1992).

The magnetic-field direction, projected on the plane of the sky, can be measured because spinning, aspherical grains tend to align their spin axes with the magnetic-field direction (see Lazarian et al 1997 for a list of mechanisms). Then the dust grains absorb and emit preferentially in the plane perpendicular to the field. Consequently, background starlight will be preferentially polarized along
and thermal emission from the grains will be polarized perpendicular to $B_\perp$ (Hildebrand 1988). Goodman (1996) has shown that the grains that polarize background starlight do not trace the field very deeply into the cloud, but maps of polarized emission at far-infrared, submillimeter (Schleuning 1998) and millimeter (Akeson & Carlstrom 1997, Rao et al 1998) wavelengths are beginning to provide maps of field direction deep into clouds. Line emission may also be weakly polarized under some conditions (Goldreich & Kylafis 1981), providing a potential probe of $B_\perp$ with velocity information. After many attempts, this effect has been detected recently (Greaves et al 1999).

The ionization fraction ($x_e$) is determined by chemical analysis and has been discussed by van Dishoeck and Blake (1998). Theoretically, $x_e$ should drop from about $10^{-4}$ near the outer edge of the cloud to about $10^{-8}$ in interiors shielded from UV radiation. Observational estimates of $x_e$ are converging on values around $10^{-8}$ to $10^{-7}$ in cores (de Boisanger et al 1996, Caselli et al 1998, Williams et al 1998, Bergin et al 1999).

### 3.5 Observational and Analytical Tools

Having discussed how different physical conditions are probed, I will end this section with a brief summary of the observational and analytical tools that are used. Clearly, most information on physical conditions comes from observations of molecular lines. Most of these lie at millimeter or submillimeter wavelengths, and progress in this field has been driven by the development of large single-dish telescopes operating at submillimeter wavelengths and by arrays of antennas operating interferometrically at millimeter wavelengths (Sargent & Welch 1993). The submillimeter capability has allowed the study of high-$J$ levels for excitation analysis and increased sensitivity to dust continuum emission, which rises with frequency ($S_\nu \propto \nu^2$ or faster). Studies of millimeter and submillimeter emission from dust have been greatly enhanced recently with the development of cameras on single dishes, both at millimeter wavelengths (Kreysa 1992) and at submillimeter wavelengths, with SHARC (Hunter et al 1996) and SCUBA (Cunningham et al 1994). Examples of the maps that these cameras are producing are the color plates showing the 1.3-mm emission from the $\rho$ Ophiuchi region (Motte et al 1998), shown in Figure 1 (color), and the 850-$\mu$m and 450-$\mu$m emission from the ridge in Orion (L1641) (Johnstone & Bally 1999), shown in Figure 2 (color).

Interferometric arrays, operating at millimeter wavelengths, have provided unprecedented angular resolution (now better than 1") maps of both molecular-line and continuum emission. They are particularly critical for separating the continuum emission from a disk and the envelope and for studying deeply embedded binaries (e.g. Looney et al 1997, Figure 3). Complementary information has been provided in the infrared, with near-infrared star counting (Lada et al 1994, 1999), near-infrared and mid-infrared spectroscopy of rovibrational transitions (e.g. Mitchell et al 1990, Evans et al 1991, Carr et al 1995, van Dishoeck et al 1998), and far-infrared continuum and spectral-line studies (e.g. Haas et al 1995). Early results from the Infrared Space Observatory can be found in Yun & Liseau (1998).
Figure 1  Map of 1.3-mm dust continuum emission covering about 2 pc in the ρ Ophiuchi cloud, with a resolution of 15′′ (Motte et al 1998). The emission is proportional to column density, and the lowest contour corresponds to $N \sim 1.4 \times 10^{22} \text{ cm}^{-2}$ or $A_V \sim 14$ mag. Contour levels increase in spacing at higher levels (see Motte et al 1998 for details). The highest contour implies $A_V \sim 780$ mag.
The 850-\(\mu\m\) emission and 450- to 850-\(\mu\m\) spectral index distribution, covering about 7 pc with a resolution of 14" at the northern end of the Orion A (L1641) molecular cloud (Johnstone & Bally 1999). The Orion Nebula is located directly in front of the strong emission at the center of the image. (Left) The 850-\(\mu\m\) image showing the observed flux from −0.1 to 2 Jy/beam with a linear transfer function. The highest flux level corresponds roughly to \(A_V \sim 320\) mag if \(T_K = 20\) K. (Center) The 850-\(\mu\m\) image showing the observed flux from 100 mJy/beam to 20 Jy/beam with a logarithmic transfer function. (Right) The 450- to 850-\(\mu\m\) spectral index in the range 2–6 with a linear transfer function.

**Figure 2**
The analytical tools for molecular-cloud studies have grown gradually in sophistication. Early studies assumed LTE excitation, an approximation that is still used in some studies of CO isotopomers, but it is clearly invalid for other species. Studies of excitation require solution of the statistical equilibrium equations (Goldsmith 1972). Goldreich & Kwan (1974) pointed out that photon trapping will increase the average $T_{\text{ex}}$ and provided a way of including its effects that was manageable with the limited computer resources of that time: the LVG approximation. Tied originally to their picture of collapsing clouds, this approximation allowed one to treat the radiative transport locally. Long after the overall collapse scenario had been discarded, the LVG method has remained in use, providing a quick way to include trapping, at least approximately. In parallel, more computationally intensive codes were developed for microturbulent clouds, in which photons emitted anywhere in the cloud could affect excitation anywhere else (e.g. Lucas 1974).

The microturbulent and LVG assumptions are the two extremes, and real clouds probably lie between. For modest optical depths, the conclusions of the two methods differ by factors of $\sim 3$, comparable to uncertainties caused by uncertain geometry (White 1977, Snell 1981). These methods are still useful in some situations, but they are gradually being supplanted by more flexible radiative transport codes, using either the Monte Carlo technique (Bernes 1979, Choi et al 1995, Park & Hong 1998, Juvela 1997) or $\Lambda$-iteration (Dickel & Auer 1994, Yates et al 1997, Wiesemeyer 1999). Some of these codes allow variations in the velocity, density, and temperature fields, nonspherical geometries, clumps, etc. Of course, increased flexibility means more free parameters and the need for more extensive observations to constrain them.

Similar developments have occurred in the area of dust continuum emission. Since stellar photons are primarily at wavelengths at which dust is quite opaque, a radiative transport code is needed to compute dust temperatures as a function of distance from a stellar heat source (Egan et al 1988, Manske & Henning 1998). For clouds without embedded stars or protostars, only the interstellar radiation field heats the dust; $T_D$ can get very low (5–10 K) in centers of opaque clouds (Leung 1975). Embedded sources heat clouds internally: in clouds opaque to the stellar radiation, it is absorbed close to the source and reradiated at longer wavelengths. Once the energy is carried primarily by photons at wavelengths where the dust is less opaque, the temperature distribution relaxes to the optically thin limit (Doty & Leung 1994):

$$T_D(r) \propto L^{q/2} r^{-q},$$

where $L$ is the luminosity of the source and $q = 2/(\beta + 4)$, assuming $\kappa(\nu) \propto \nu^\beta$.

4. FORMATION OF ISOLATED LOW-MASS STARS

Many low-mass stars actually form in regions of high-mass star formation, where clustered formation is the rule (Elmegreen 1985, Lada 1992, McCaughrean & Stauffer 1994). The focus here is on regions where we can isolate the
individual star-forming events, and these are almost inevitably forming low-mass stars.

4.1 Theoretical Issues

The theory of isolated star formation has been developed in some detail. It relies on the existence of relatively isolated regions of enhanced density that can collapse toward a single center, although processes at smaller scales may cause binaries or multiples to form. One issue then is whether isolated regions suitable for forming individual, low-mass stars are clearly identifiable. The ability to separate these from the rest of the cloud underlies the distinction between sterile and fertile parts of clouds (Section 1).

Because of the enormous compression needed, gravitational collapse plays a key role in all star formation theories. In most cases, only a part of the cloud collapses, and theories differ on how this part is distinguished from the larger cloud. Is it brought to the verge of collapse by an impulsive event, like a shock wave (Elmegreen & Lada 1977) or a collision between clouds or clumps (Loren 1976), or is the process gradual? Among gradual processes, the decay of turbulence and ambipolar diffusion are leading contenders. If the decay of turbulence leaves the cloud in a subcritical state ($M < M_B$), then a relatively long period of ambipolar diffusion is needed before dynamical collapse can proceed (Section 2). If the cloud is supercritical ($M > M_B$), then the magnetic field alone cannot stop the collapse (e.g. Mestel 1985). If turbulence does not prevent it, a rapid collapse ensues, and fragmentation is likely. Shu et al (1987a,b) suggested that the subcritical case describes isolated low-mass star formation, while the supercritical case describes high-mass and clustered star formation. Recently, Nakano (1998) has argued that star formation in subcritical cores via ambipolar diffusion is implausible; instead he favors dissipation of turbulence as the controlling factor. For the present section, the questions are whether there is evidence that isolated, low-mass stars form in subcritical regions and what the status of turbulence in these cores is.

Rotation could in principle support clouds against collapse, except along the rotation axis (Field 1978). Even if rotation does not prevent the collapse, it is likely to be amplified during collapse, leading at some point to rotation speeds able to affect the collapse. In particular, rotation is usually invoked to produce binaries or multiple systems on small scales. What do we know about rotation rates on large scales and how the rotation is amplified during collapse? Is there any correlation between rotation and the formation of binaries observationally? If rotation controls whether binaries form, can we understand why collapse leads to binary formation roughly half the time? It is clear that both magnetic flux and angular momentum must be redistributed during collapse to produce stars with reasonable fields and rotation rates, and these processes will affect the formation of binaries and protoplanetary disks. Some of these questions will be addressed in the next sections on globules and cores; while others will be discussed in the context of testing specific theories.
4.2 Globules and Cores: Overall Properties

Nearby small dark clouds or globules are natural places to look for isolated star formation (Bok & Reilly 1947). A catalog of 248 globules (Clemens & Barvainis 1988) has provided the basis for many studies. Yun & Clemens (1990) found that 23\% of the CB globules appear to contain embedded infrared sources, with spectral-energy distributions typical of star-forming regions (Yun 1993). About one-third of the globules with embedded sources have evidence of outflows (Yun & Clemens 1992, Henning & Launhardt 1998). Clearly, star formation does occur in isolated globules.

Within the larger dark clouds, one can identify numerous regions of high opacity (e.g. Myers et al 1983), commonly called cores (Myers 1985). Surveys of such regions in low-excitation lines of NH$_3$ (e.g. Benson & Myers 1989) led to the picture of an isolated core within a larger cloud, which then might pursue its course toward star formation in relative isolation from the rest of the cloud. Most intriguing was the fact that the NH$_3$ line widths in many of these cores indicated that the turbulence was subsonic (Myers 1983); in some cores, thermal broadening of NH$_3$ lines even dominated over turbulent broadening (Myers & Benson 1983, Fuller & Myers 1993). Although later studies in other lines indicated a more complex dynamical situation (Zhou et al 1989, Butner et al 1995), the NH$_3$ data provided observational support for theories describing the collapse of isothermal spheres (Shu 1977). The discovery of IRAS sources in half of these cores (Beichman et al 1986) indicated that they were indeed sites of star formation. The observational and theoretical developments were synthesized into an influential paradigm for low-mass star formation (Shu et al 1987a; Section 4.5 below).

Globules would appear to be an ideal sample for measuring sizes because the effects of the environment are minimized by their isolation, but distances are uncertain. Based on the angular size of the optical images and an assumed average distance of 600 pc (Clemens & Barvainis 1988), the mean size $\langle l \rangle = 0.7$ pc. A subsample of these with distance estimates were mapped in molecular lines, yielding much smaller average sizes: $\langle l \rangle = 0.33 \pm 0.15$ pc for a sample of 6 “typical” globules mapped in CS (Launhardt et al 1998); maps of the same globules in C$^{18}$O $J = 2 \rightarrow 1$ (Wang et al 1995) give sizes smaller by a factor of 2.9 $\pm$ 1.6. A sample of 11 globules in the southern sky mapped in NH$_3$ (Bourke et al 1995) have $\langle l \rangle = 0.21 \pm 0.08$ pc.

Cores in nearby dark clouds have the advantage of having well-determined distances; the main issue is how clearly they stand out from the bulk of the molecular cloud. Gregersen (1998) found that some known cores are barely visible above the general cloud emission in the C$^{18}$O $J = 1 \rightarrow 0$ line. The mean size of a sample of 16 cores mapped in NH$_3$ is 0.15 pc, whereas CS $J = 2 \rightarrow 1$ gives 0.27 pc, and C$^{18}$O $J = 1 \rightarrow 0$ gives 0.36 pc (Myers et al 1991). These differences may reflect the effects of opacity, chemistry, and density structure.

Globules are generally not spherical. By fitting the opaque cores with ellipses, Clemens & Barvainis (1988) found a mean aspect ratio $(a/b)$ of 2.0. Measurements
of aspect ratio in tracers of reasonably dense gas toward globules give \( \langle a/b \rangle \sim 1.5 - 2 \) (Wang et al 1995, Bourke et al 1995), and cores in larger clouds have \( \langle a/b \rangle \sim 2 \) (Myers et al 1991). Myers et al (1991) and Ryden (1996) have argued that the underlying three-dimensional shapes were more likely to be prolate, with axial ratios of \( \sim 2 \), than oblate, for which axial ratios of 3–10 were needed. However, toroids may also be able to match the data because of their central density minima (Li & Shu 1996).

The uncertainties in size are reflected directly into uncertainties in mass. For the sample of globules mapped by Bourke et al (1995) in NH\(_3\), \( \langle M_N \rangle = 4 \pm 1 \, \text{M}_\odot \), compared with \( 10 \pm 2 \, \text{M}_\odot \) for cores. Larger masses are obtained from other tracers. For the sample of globules studied by Launhardt et al (1998), \( \langle M_V \rangle = 26 \pm 12 \) based on CS \( J = 2 \rightarrow 1 \) and \( 10 \pm 6 \), based on C\(^{18}\)O \( J = 2 \rightarrow 1 \). Studies of the cores in larger clouds found similar ranges and differences among tracers (e.g. Fuller 1989, Zhou et al 1994a). A series of studies of the Taurus cloud complex has provided an unbiased survey of cores with known distance identified by C\(^{18}\)O \( J = 1 \rightarrow 0 \) maps. Starting from a large-scale map of \(^{13}\)CO \( J = 1 \rightarrow 0 \) (Mizuno et al 1995), Onishi et al (1996) covered 90% of the area with \( N \geq 3.5 \times 10^{21} \) with a map of C\(^{18}\)O \( J = 1 \rightarrow 0 \) with 0.1 pc resolution. They identified 40 cores with \( \langle l \rangle = 0.46 \, \text{pc} \), \( \langle a/b \rangle = 1.8 \), and \( \langle M_N \rangle = 23 \, \text{M}_\odot \). The sizes extended over a range of a factor of 6 and masses over a factor of 80. Comparing these cores to the distribution of T Tauri stars, infrared sources, and H\(^{13}\)CO\(^+\) emission, Onishi et al (1998) found that all cores with \( N > 8 \times 10^{21} \, \text{cm}^{-2} \) are associated with H\(^{13}\)CO\(^+\) emission and/or cold IRAS sources. In addition, the larger cores always contained multiple objects. They concluded that the core mass per star-forming event is relatively constant at 11 M\(_\odot\).

It is clear that characterizing globules and cores by a typical size and mass is an oversimplification. First, they come in a range of sizes that is probably just the low end of the general distribution of cloud sizes. Second, the size and mass depend strongly on the tracer and method used to measure them. If we ignore these caveats, it is probably fair to say that most of these regions have sizes measured in tracers of reasonably dense gas in the range of a few tenths of a pc and masses of \( < 100 \, \text{M}_\odot \), with more small, low-mass cores than massive ones. The larger cores tend to be fragmented, so that the mass of gas with \( n \geq 10^4 \, \text{cm}^{-3} \) tends toward 10 M\(_\odot\), within a factor of 2. Star formation may occur when the column density exceeds \( 8 \times 10^{21} \, \text{cm}^{-2} \), corresponding in this case to \( n \sim 10^4 \, \text{cm}^{-3} \).

### 4.3 Globules and Cores: Internal Conditions

If the sizes and masses of globules and cores are poorly defined, at least the temperatures seem well understood. Early CO observations (Dickman 1975) showed that the darker globules are cold \( (T_K \sim 10 \, \text{K}) \), as expected for regions with only cosmic-ray heating. Similar results were found from NH\(_3\) (Martin & Barrett 1978, Myers & Benson 1983, Bourke et al 1995). Clemens et al (1991) showed the distribution of CO temperatures for a large sample of globules; the main peak
corresponded to $T_K = 8.5 \text{ K}$, with a small tail to higher $T_K$. Determination of the dust temperature was more difficult, but Keene (1981) measured $T_D = 13–16 \text{ K}$ in B133, a starless core. More recently, Ward-Thompson et al (1998) used Infrared Space Observatory data to measure $T_D = 13 \text{ K}$ in another starless core. These results are similar to predictions for cores heated by the interstellar radiation field (Leung 1975), although $T_D$ is expected to be lower in the deep interiors.

A sample of starless globules with $A_V \sim 1–2 \text{ mag}$ produced no detections of NH$_3$ (Kane et al 1994), but surveys of H$_2$CO (Wang et al 1995) and CS (Launhardt et al 1998, Henning & Launhardt 1998) toward more opaque globules indicate that dense gas is present in some. The detection rate of CS $J = 2 \rightarrow 1$ emission was much higher in globules with infrared sources. Butner et al (1995) analyzed multiple transitions of DCO$^+$ in 18 low-mass cores, finding $\langle \log n(\text{cm}^{-3}) \rangle \simeq 5$, with a tendency to slightly higher values in the cores with infrared sources. Thus, gas still denser than the $\langle \log n(\text{cm}^{-3}) \rangle \simeq 4$ gas traced by NH$_3$ exists in these cores.

Discussion of the kinematics of globules and cores has often focused on the relationship between line width ($\Delta v$) and size ($l$ or $R$). This relation is much less clearly established for cores within a single cloud than is the relation for clouds as a whole (Section 3.3), and it may have a different origin (Myers 1985). Goodman et al (1998) have distinguished four types of line width-size relationships. Most studies have used Goodman Type-1 (multitracer, multicore) relations, but it is difficult to distinguish different causes in such relations. Goodman Type-2 (single-tracer, multicore) relations within a single cloud would reveal whether the virial masses of cores are reliable. Interestingly, the most systematic study of cores in a single cloud found no correlation in 24 cores in Taurus mapped in C$^{18}$O $J = 1 \rightarrow 0$ ($\gamma = 0.0 \pm 0.2$), but the range of sizes (0.13 to 0.4 pc) may have been insufficient (Onishi et al 1996).

To study the kinematics of individual cores, the most useful relations are Goodman Types-3 (multitracer, single-core) and -4 (single-tracer, single-core) relations. In these, a central position is defined, either by an infrared source or a line peak. A Type-3 relationship using NH$_3$, C$^{18}$O $J = 1 \rightarrow 0$, and CS $J = 2 \rightarrow 1$ lines was explored by Fuller & Myers (1992), who found $\Delta v \propto R',$ with $R$ the radius of the half-power contour. Caselli & Myers (1995) added $^{13}$CO $J = 1 \rightarrow 0$ data and constructed a Type-1 relation for eight starless cores, after removing the thermal broadening. The mean $\gamma$ was $0.53 \pm 0.07$ with a correlation coefficient of 0.81. However, both these relationships depend strongly on the fact that the NH$_3$ lines have small $\Delta v$ and $R$. Some other species such as DCO$^+$ also have narrow lines and small sizes, but DCO$^+$ emission has much wider lines over a similar map size (Butner et al 1995), raising the possibility that chemical effects cause different molecules to trace different kinematic regimes within the same overall core. Goodman et al (1998) suggest that the DCO$^+$ is excited in a region outside the NH$_3$ region and that the size of the DCO$^+$ region is underestimated. On the other hand, some chemical simulations indicate that NH$_3$ will deplete in dense cores while ions like DCO$^+$ will not (Rawlings et al 1992), suggesting the opposite solution.
A way to avoid such effects is to use a Type-4 relation, searching for a correlation between $\Delta v_{NT}$ as spectra are averaged in rings of larger size, although line of sight confusion cannot be avoided as one gives up the ability to tune the density sensitivity. This method has almost never been applied to tracers of dense gas, but Goodman et al (1998) use an indirect method to obtain a Type-4 relation for three clouds in OH, C$^{18}$O, and NH$_3$. The relations are very flat ($\gamma = 0.1$–0.3), and $\gamma \neq 0$ has statistical significance only for OH, which traces the least dense gas. In particular, NH$_3$ shows no significant Type-4 relation, having narrow lines on every scale (see also Barranco & Goodman 1998). Goodman et al (1998) interpret these results in terms of a “transition to coherence” at the scale of 0.1–0.2 pc from the center of a dense core. Inside that radius, the turbulence becomes subsonic and no longer decreases with size (Barranco & Goodman 1998). Although this picture accords nicely with the idea that cores can be distinguished from the surroundings and treated as “units” in low-mass star formation, the discrepancy between values of $\Delta v$ measured in different tracers of the dense core (cf Butner et al 1995) indicates that caution is required in interpreting the NH$_3$ data.

Rotation can be detected in some low-mass cores, but the ratio of rotational to gravitational energy has a typical value of 0.02 on scales of 0.1 pc (Goodman et al 1993). The inferred rotation axes are not correlated with the orientation of cloud elongation, again suggesting that rotation is not dynamically important on the scale of 0.1 pc. Ohashi et al (1997a) find evidence in several star-forming cores for a transition at $r \sim 0.03$ pc, inside of which the specific angular momentum appears to be constant at $\sim 10^{-3}$ km s$^{-1}$ pc down to scales of $\sim 200$ AU.

Knowledge of the magnetic-field strength in cores and globules would be extremely valuable in assessing whether they are subcritical or supercritical. Unfortunately, Zeeman measurements of these regions are extremely difficult because they must be done with emission, unless there is a chance alignment with a background radio source. Crutcher et al (1993) detected Zeeman splitting in OH in only 1 of 12 positions in nearby clouds. Statistical analysis of the detection and the upper limits, including the effects of random orientation of the field, led to the conclusion that the data could not falsify the hypothesis that the clouds were subcritical. Another problem is that the OH emission probes relatively low densities ($n \sim 10^3$ cm$^{-3}$). Attempts to use CN to probe denser gas produced upper limits that were less than expected for subcritical clouds, but the small sample size and other uncertainties again prevented a definitive conclusion (Crutcher et al 1996). Improved sensitivity and larger samples are crucial to progress in this field. At present, no clear examples of subcritical cores have been found (Crutcher 1999a), but uncertainties are sufficient to allow this possibility.

Onishi et al (1996) found that the major axis of the cores they identified in Taurus tended to be perpendicular to the optical polarization vectors and hence $B \perp$. Counterexamples are known in other regions (e.g. Vrba et al 1976) and the fact that optical polarization does not trace the dense portions of clouds (Goodman 1996) suggests that this result be treated cautiously. Further studies of $B \perp$ using dust emission at long wavelengths are clearly needed.
The median ionization fraction of 23 low-mass cores is $9 \times 10^{-8}$, with a range of $\log x_e$ of $-7.5$ to $-6.5$, with typical uncertainties of a factor of 0.5 in the log (Williams et al 1998). Cores with stars do not differ significantly in $x_e$ from cores without stars, consistent with cosmic-ray ionization. For a cloud with $n = 10^4 \text{ cm}^{-3}$, the ambipolar diffusion timescale is $t_{AD} \sim 7 \times 10^6 \text{ years} \sim 20t_{ff}$. If the cores are subcritical, they will evolve much more slowly than a free-fall time. Recent comparisons of the line profiles of ionized and neutral species have been interpreted as setting an upper limit on the ion-neutral drift velocity of 0.03 km s$^{-1}$, consistent with that expected from ambipolar diffusion (Benson et al 1998).

To summarize the last two subsections, there is considerable evidence that distinct cores can be identified, both as isolated globules and as cores within larger clouds. Although there is a substantial range of properties, scales of 0.1 pc in size and 10 M$_\odot$ in mass seem common. The cores are cold ($T_K \sim T_D \sim 10 \text{ K}$) and contain gas with $n \sim 10^4 \text{ cm}^{-3}$, extending in some cases up to $n \sim 10^5 \text{ cm}^{-3}$. Although different molecules differ in the magnitude of the effect, these cores seem to be regions of decreased turbulence compared with the surroundings. Although no clear cases of subcritical cores have been found, the hypothesis that low-mass stars form in subcritical cores cannot be ruled out observationally. How these cores form is beyond the scope of this review, but again one can imagine two distinct scenarios: ambipolar diffusion brings an initially subcritical core to a supercritical state, or dissipation of turbulence plays a similar role in a core originally supported by turbulence (Myers & Lazarian 1998). In the latter picture, cores may build up from accretion of smaller diffuse elements (Kuiper et al 1996), perhaps the structures inferred by Falgarone et al (1998).

### 4.4 Classification of Sources and Evolutionary Scenarios

The IRAS survey provided spectral energy distributions over a wide wavelength range for many cores (e.g., Beichman et al 1986), leading to a classification scheme for infrared sources. In the original scheme (Lada & Wilking 1984, Lada 1987), the spectral index between 2 $\mu$m and the longest observed wavelength was used to divide sources into three Classes, designated by roman numerals, with Class I indicating the most emission at long wavelengths. These classes rapidly became identified with stages in the emerging theoretical paradigm (Shu et al 1987a): Class-I sources are believed to be undergoing infall with simultaneous bipolar outflow, Class-II sources are typically visible T Tauri stars with disks and winds, and Class-III sources have accreted or dissipated most of the material, leaving a pre–main-sequence star, possibly with planets (Adams et al 1987, Lada 1991).

More recently, submillimeter continuum observations have revealed a large number of sources with emission peaking at still longer wavelengths. Some of these new sources also have infrared sources and powerful bipolar outflows, indicating that a central object has formed; these have been designated Class 0 (André et al 1993). André & Montmerle (1994) argued that Class-0 sources represent the primary infall stage, in which there is still more circumstellar than stellar matter.
Outflows appear to be most intense in the earliest stages, declining later (Bontemps et al 1996). Other cores with submillimeter emission have no IRAS sources and probably preceed the formation of a central object. These were found among the “starless cores” of Benson & Myers (1989), and Ward-Thompson et al (1994) referred to them as “pre-protostellar cores.” The predestination implicit in this name has made it controversial, and I use the less descriptive (and somewhat tongue-in-cheek) term, Class −1. There has also been some controversy over whether Class-0 sources are really distinct from Class-I sources or just more extreme versions. The case for Class-0 sources as a distinct stage can be found in Andrés et al (2000).

While classification has an honored history in astronomy, serious tests of theory are facilitated by continuous variables. Myers & Ladd (1993) suggested that we characterize the spectral energy distribution by the flux-weighted mean frequency, or, more suggestively, by the temperature of a black body with the same mean frequency. The latter (\(T_{\text{bol}}\)) was calculated by Chen et al (1995) for many sources, and the following boundary lines in \(T_{\text{bol}}\) were found to coincide with the traditional classes: \(T_{\text{bol}} < 70\) K for Class 0, \(70 \leq T_{\text{bol}} \leq 650\) K for Class I, and \(650 < T_{\text{bol}} \leq 2800\) K for Class II. In a crude sense, \(T_{\text{bol}}\) captures the “coolness” of the spectral energy distribution, which is related to how opaque the dust is, but it can be affected strongly by how much mid-infrared and near-infrared emission escapes and thus by geometry. Other measures, such as the ratio of emission at a submillimeter wavelength to the bolometric luminosity (\(L_{\text{smm}}/L_{\text{bol}}\)), may also be useful. One of the problems with all of these measures is that the bulk of the energy for classes earlier than II emerges at far-infrared wavelengths, where resolution has been poor. Maps of submillimeter emission are showing that many near-infrared sources are displaced from the submillimeter peaks and may have been falsely identified as Class-I sources (Motte et al 1998). Ultimately, higher spatial resolution in the far-infrared will be needed to sort out this confusion.

4.5 Detailed Theories

The recent focus on the formation of isolated, low-mass stars is at least partly due to the fast that it is more tractable theoretically than the formation of massive stars in clusters. Shu (1977) argued that collapse begins in a centrally condensed configuration and propagates outward at the sound speed (\(a\)); matter inside \(r_{\text{in}}\) is infalling after a time \(t\). Because the collapse in this model is self-similar, the structure can be specified at any time from a single solution. This situation is called inside-out collapse. In Shu’s picture, the precollapse configuration is an isothermal sphere, with \(n(r) \propto r^{-p}\) and \(p = 2\). Calculations of core formation via ambipolar diffusion gradually approach a configuration with an envelope that is close to a power law, but with a core of ever-shrinking size and mass in which \(p \sim 0\) (e.g. Mouschovias 1991). It is natural to identify the ambipolar diffusion stage with the Class −1 stage and the inside-out collapse with Class 0 to Class I. As collapse proceeds, the material inside \(r_{\text{in}}\) becomes less dense, with a power...
law approaching \( p = 1.5 \) in the inner regions, after a transition region where the density is not a power law. In addition, \( v(r) \propto r^{-0.5} \) at small \( r \).

There are many other solutions to the collapse problem (Hunter 1977, Foster & Chevalier 1993), ranging from the inside-out collapse to overall collapse (Larson 1969, Penston 1969). Henriksen et al (1997) have argued that collapse begins before the isothermal sphere is established; the inner \(( p = 0 \) core undergoes a rapid collapse that they identify with Class-0 sources. They suggest that Class-I sources represent the inside-out collapse phase, which appears only when the wave of infall has reached the \( p = 2 \) envelope.

Either rotation or magnetic fields will break spherical symmetry. Terebey et al (1984) added slow rotation of the original cloud at an angular velocity of \( \Omega \) to the inside-out collapse picture, resulting in another characteristic radius, the point where the rotation speed equals the infall speed. A rotationally supported disk should form somewhere inside this centrifugal radius (Shu et al 1987a).

\[
 r_c = \frac{G^3 M^3 \Omega^2}{16 \omega^8},
\]  

where \( M \) is the mass already in the star and disk. Because disks are implicated in all models of the ultimate source of the outflows, the formation of the disk may also signal the start of the outflow. Once material close to the rotation axis has accreted (or been blown out), all further accretion onto the star should occur through the disk.

Core formation in a magnetic field should produce a flattened structure (e.g. Fiedler & Mouschovias 1993), and Li & Shu (1996) argue that the equilibrium structure equivalent to the isothermal sphere is the isothermal toroid. Useful insights into the collapse of a magnetized cloud have resulted from calculations in spherical geometry (Safier et al 1997, Li 1998) or for thin disks (Ciolek & Königl 1998). Some calculations of collapse in two dimensions have been done (e.g. Fiedler & Mouschovias 1993). A magnetically channeled, flattened structure may appear; this has been called a pseudodisk (Galli & Shu 1993a,b) to distinguish it from the rotationally supported disk. In this picture, material would flow into a pseudodisk at a scale of \( \sim 1000 \) AU before becoming rotationally supported on the scale of \( r_c \). The breaking of spherical symmetry on scales of \( 1000 \) AU may explain some of the larger structures seen in some regions (see Mundy et al 2000 for a review).

Ultimately, theory should be able to predict the conditions that lead to binary formation, but this is not currently possible. Steps toward this goal can be seen in numerical calculations of collapse with rotation (e.g. Bonnell & Bastien 1993, Truelove et al 1998, Boss 1998). Rotation and magnetic fields have been combined in a series of calculations by Basu & Mouschovias (1995 and references therein); Basu (1998) has considered the effects of magnetic fields on the formation of rotating disks.

Theoretical models make predictions that are testable, at least in principle. In the simplest picture of the inside-out collapse of the rotationless, nonmagnetic
isothermal sphere, the theory predicts all of the density and velocity structure with
only the sound speed as a free parameter. Rotation adds $\Omega$, and magnetic fields add
a reference field or equivalent as additional parameters. Departure from spherical
symmetry adds the additional observational parameter of viewing angle. Conse-
sequently, observational tests have focused primarily on testing the simplest models.

4.6 Tests of Evolutionary Hypotheses and Theory

Both the empirical evolutionary sequence based on the class system and the detailed
theoretical predictions can be tested by detailed observations. One can compute
the expected changes in the continuum emission as a function of time for a par-
ticular model. Examples include plots of $L$ versus $A_V$ (Adams 1990), $L$ versus
$T_{bol}$ (Myers et al 1998), and $L_{mm}$ versus $L$ (Saraceno et al 1996). For example,
as time goes on, $A_V$ decreases, $T_{bol}$ increases, and $L$ reaches a peak and declines.
At present the models are somewhat idealized and simplified, and different dust
opacities need to be considered. Comparison of the number of objects observed
in various parts of these diagrams with those expected from lifetime considera-
tions can provide an overall check on evolutionary scenarios and provide age esti-
mates for objects in different classes (e.g. Andrê et al 2000). One can also test the
models against observations of particular objects. However, models of source struc-
ture constrained only by the spectral-energy distribution are not unique (Butner
et al 1991, Men’shchikov & Henning 1997). Observational determination of $n(r)$
and $v(r)$ can apply more stringent tests.

Maps of continuum emission from dust can trace the column density as a func-
tion of radius quite effectively, if the temperature distribution is known. With an
assumption about geometry, this information can be related to $n(r)$. For the Class
$-1$ sources, with no central object, the core should be isothermal ($T_D \sim 5–10$ K)
or warmer on the outside if exposed to the interstellar radiation field (Leung
1975, Spencer & Leung 1978). New results from the Infrared Space Observatory
will put tighter limits on possible internal energy sources (e.g. Ward-Thompson
et al 1998, Andrê et al 2000). Based on small maps of submillimeter emission,
Ward-Thompson et al (1994) found that Class $-1$ sources were not characterized
by single power laws in column density; they fit the distributions with broken
power laws, indicating a shallower distribution closer to the center. This distri-
bution appears consistent with the interpretation that these are cores still forming
by ambipolar diffusion. Maps at 1.3 mm (Andrê et al 1996, Ward-Thompson
et al 1999) confirm the early results: the column density is quite constant in
an inner region ($r < 3000–4000$ AU), with $M \sim 0.7 M_\odot$. SCUBA maps of
these sources are just becoming available, but they suggest similar conclusions
(D Ward-Thompson, personal communication; Shirley et al 1998). In addition,
some of the cores are filamentary and fragmented (Ward-Thompson et al 1999).
Citing these observed properties, together with a statistical argument regarding
lifetimes, Ward-Thompson et al (1999) now argue that ambipolar diffusion in
subcritical cores does not match the data (see also Andrê et al 2000).
For cores with central sources (Class $\geq -1$), $T_D(r)$ will decline with radius from the source. If the emission is in the Rayleigh-Jeans limit, $I_\nu \propto T_Dk(\nu)N$.

If $k(\nu)$ is not a function of $r$, $I_\nu(\theta) \propto \int T_D(r)n(r)dl$, where the integration is performed along the line of sight ($dl$). If one avoids the central beam and any outer cut-off, assumes the optically thin expression for $T_D(r) \propto r^{-q}$, and fits a power law to $I_\nu(\theta) \propto \theta^{-m}$, then $p = m + 1 - q$ (Adams 1991, Ladd et al 1991). With a proper calculation of $T_D(r)$ and convolution with the beam, one can include all of the information (Adams 1991). This technique has been applied in the far-infrared (Butner et al 1991), but it is most useful at longer wavelengths. Ladd et al (1991) found $p = 1.7 \pm 0.3$ in two cores, assuming $q = 0.4$, as expected for $\beta = 1$ (Equation 14). Results so far are roughly consistent with theoretical models, but results in this area from the new submillimeter cameras will “explode” about the time this review goes to press.

Another issue arises for cores with central objects. If a circumstellar disk contributes significantly to the emission in the central beam, it will increase the fitted value of $m$. Disks contribute more importantly at longer wavelengths, so the disk contribution is more important at millimeter wavelengths (e.g. Chandler et al 1995). Luckily, interferometers are available at those wavelengths, and observations with a wide range of antenna spacings can separate the contributions of a disk and envelope. Application of this technique by Looney et al (1997) to L1551 IRS5, a Class-I source, reveals very complex structures (Figure 3): binary circumstellar disks (cf Rodríguez et al 1998), a circumbinary structure (perhaps a pseudodisk), and an envelope with a density distribution consistent with a power law ($p = 1.5–2$). This technique promises to be very fruitful in tracing the flow of matter from envelope to disk. Early results indicated that disks are more prominent in more evolved (Class-II) systems (Ohashi et al 1996), but compact structures are detectable in some younger systems (Terebey et al 1993). Higher-resolution observations and careful analysis will be needed to distinguish envelopes, pseudodisks, and Keplerian disks (see Mundy et al 2000 for a review). At the moment, one can say only that disks in the Class-0 stage are not significantly more massive than disks in later classes (Mundy et al 2000). Meanwhile, the interferometric data confirm the tendency of envelope mass to decrease with class number inferred from single-dish data (Mundy et al 2000).

Similar techniques have been used for maps of molecular line emission. For example, $^{13}$CO emission has been used to trace column density in the outer regions of dark clouds. With an assumption of spherical symmetry, the results favor $p \sim 2$ in most clouds (Snell 1981, Arquilla & Goldsmith 1985). The $^{13}$CO lines become optically thick in the inner regions; studies with higher spatial resolution in rarer isotopomers, like $^{18}$O or $^{17}$O, tend to show somewhat more shallow density distributions than expected with the standard model (Zhou et al 1994b, Wang et al 1995). Depletion in the dense, cold cores may still confuse matters (e.g. Kuiper et al 1996, Section 3.1). Addressing the question of evolution, Ladd et al (1998) used two transitions of $^{18}$O and $^{17}$O to show that $N$ toward the central source declines with $T_{bol}$, with a power between 0.4 and 1.0. To reproduce the inferred
Figure 3  Observed visibilities of L1551 IRS 5 at 2.7 mm, binned in annuli (open squares with error bars), are plotted versus the projected baseline in units of $10^3$ times the wavelength. Different models are shown in each panel by the small boxes. Panel a has a model with only a Gaussian source of radius 80 AU; panel b has a model with two point sources constrained to match the map; panel c adds a truncated power law ($p = 1.5$, $q = 0.5$) envelope to the two point sources; panel d adds to the previous components a circumbinary structure, represented by a Gaussian. In the final optimization (panel d), the envelope has a mass of 0.28 $M_\odot$ and an outer radius of 1100 AU, the circumbinary structure has a mass of 0.04 $M_\odot$, and the circumstellar disk masses are 0.024 and 0.009 $M_\odot$ (Looney et al 1997).

rapid decrease in mass with time, they suggest higher early mass loss than predicted by the standard model.

By observing a series of lines of different critical density, modeling those lines with a particular cloud model and appropriate radiative transport, and predicting the emission into the beams used for the observations, one can constrain the run of density more directly. Studies using two transitions of H$_2$CO have again supported $p = 2 \pm 0.5$ on relatively large scales (Loren et al 1983, Fulkerson & Clark 1984). When interferometry of H$_2$CO was used to improve the resolution on one core, $p$ appeared to decrease at small $r$ (Zhou et al 1990), in agreement with the model of Shu (1977). Much of the recent work on this topic has involved testing of
detailed collapse models, including velocity fields and the complete density law, rather than a single power law, as described in the next section.

4.7 Collapse


Zhou et al (1993) showed that several lines of CS and H2CO observed towards B335, a globule with a Class-0 source, could be fitted very well by using the exact $n(r)$ and $v(r)$ of the inside-out collapse model. Using a more self-consistent radiative transport code, Choi et al (1995) found slightly different best-fit parameters. With a sound speed determined from lines away from the collapse region, the only free parameters were the time since collapse began and the abundance of each molecule. With several lines of each molecule, the problem is quite constrained (Figure 4). This work was important in gaining acceptance for the idea that collapse had finally been seen.

Examination of the line profiles in Figure 4 reveals that most are strongly self-absorbed. Recall that the overall collapse idea of Goldreich & Kwan (1974) was designed to avoid self-absorbed profiles. The difference is that Goldreich & Kwan assumed that $v(r) \propto r$, so that every velocity corresponded to a single point along the line of sight. In contrast, the inside-out collapse model predicts $v(r) \propto r^{-0.5}$ inside a static envelope. If the line has substantial opacity in the static envelope, it will produce a narrow self-absorption at the velocity centroid of the core (Figure 5). The other striking feature of the spectra in Figure 4 is that the blue-shifted peak is stronger than the red-shifted peak. This blue profile occurs because the $v(r) \propto r^{-0.5}$ velocity field has two points along any line of sight with the same Doppler shift (Figure 6). For a centrally peaked temperature and density distribution, lines with high critical densities will have higher $T_{ex}$ at the point closer to the center. If the line has sufficient opacity at the relevant point in the cloud, the high $T_{ex}$ point in the red peak will be obscured by the lower $T_{ex}$ one, making the red peak weaker than the blue peak (Figure 6). Thus a collapsing cloud with a velocity and density gradient similar to those in the inside-out collapse model will produce blue profiles in lines with suitable excitation and opacity properties. A double-peaked profile with a stronger blue peak or a blue-skewed profile relative to an optically thin line then becomes a signature of collapse. These features were discussed by Zhou & Evans (1994) and, in a more limited context, by Snell & Loren (1977) and Leung & Brown (1977).
Figure 4 Line profiles of H$_2$CO and CS emission (solid histograms) toward B335 and the best-fitting model (dashed lines). The model line profiles were calculated with a Monte Carlo code, including non-LTE excitation and trapping, with an input density and velocity field taken directly from the collapse model of Shu (1977) and a temperature field calculated with a separate dust radiation transport code. The best-fitting model has an infall radius of 0.03 pc (Choi et al 1995).

Of course, the collapse interpretation of a blue profile is not unique. Such profiles can be produced in a variety of ways. To be a plausible candidate for collapse, a core must also show these features: an optically thin line must peak between the two peaks of the opaque line; the strength and skewness should peak on the central source; and the two peaks should not be caused by clumps in an outflow. The optically thin line is particularly crucial, because two cloud components, for example, colliding fragments, could produce the double-peaked blue profile, but they would also produce a double-peaked profile in the optically thin line.

Rotation, combined with self-absorption, can create a line profile like that of collapse (Menten et al 1987, Adelson & Leung 1988), but toward the center of rotation, the line would be symmetric (Zhou 1995). Rotating collapse can cause
Figure 5  The origin of various parts of the line profile for a cloud undergoing inside-out collapse. The static envelope outside $r_{inf}$ produces the central self-absorption dip, the blue peak comes from the back of the cloud, and the red peak from the front of the cloud. The faster collapse near the center produces line wings, but these are usually confused by outflow wings.

the line profiles to shift from blue to red-skewed on either side of the rotation axis, with the sign of the effect depending on how the rotation varies with radius (Zhou 1995). Maps of the line centroid can be used to separate rotation from collapse (Adelson & Leung 1988, Walker et al 1994).

To turn a collapse candidate into a believable case of collapse, one has to map the line profiles, account for the effects of outflows, model rotation if present, and show that a collapse model fits the line profiles. To date this has been done only for a few sources: B335 (Zhou et al 1993, Choi et al 1995), L1527 (Myers et al 1995,
Figure 6 A schematic explanation of why line profiles of optically thick, high-excitation lines are skewed to the blue in a collapsing cloud. The *ovals* are loci of constant line-of-sight velocity, for $v(r) \propto r^{-0.5}$. Each line of sight intersects these loci at two points. The point closer to the center will have a higher $T_{\text{ex}}$, especially in lines that are hard to excite, so that $T_{\text{ex}}(R_2) > T_{\text{ex}}(R_1)$ and $T_{\text{ex}}(B_2) > T_{\text{ex}}(B_1)$. If the line is sufficiently opaque, the point $R_1$ will obscure the brighter $R_2$, but $B_2$ lies in front of $B_1$. The result is a profile with the blue peak stronger than the red peak (Zhou & Evans 1994).

Zhou et al 1996, Gregersen et al 1997), and IRAS 16293 (Zhou 1995, Narayanan et al 1998). Of this group, only IRAS 16293, rotating about 20 times faster than B335, is known to be a binary (Wootten 1989, Mundy et al 1992), supporting the idea that faster rotation is more likely to produce a binary. Mathieu (1994) reviews binarity in the pre–main-sequence stage, and Mundy et al (2000) discuss recent evidence on the earlier stages.

Interferometric observations have also revealed infall motions and rotational motions on scales of $\sim1000$ AU in several sources (e.g. Ohashi et al 1997a, Momose et al 1998). Such studies can reveal how matter makes the transition from infall to a rotating disk. Inevitably, irregularities in the density and velocity fields will confuse matters in real sources, and these may be more noticeable with interferometers. Outflows are particularly troublesome (Hogerheijde et al 1998). Extreme blue/red ratios are seen in interferometric observations of HCO$^+$ and HCN $J = 1 \rightarrow 0$ lines, which are difficult to reproduce with standard models.
(Choi et al 1999). Even in B335, the best case for collapse, Velusamy et al (1995) found evidence for clumpy structure within the overall gradients. In addition, very high-resolution observations of CS $J = 5 \rightarrow 4$ emission toward B335 are not consistent with predicted line profiles very close to the forming star (DJ Wilner, PC Myers, D Mardones, M Tafalla, manuscript in preparation); either CS is highly depleted in the infalling gas, or the velocity or density fields depart from the model.

If, for the sake of argument, we accept a blue profile as a collapsing core, can we see any evolutionary trends? A number of surveys for blue profiles have been undertaken recently. Gregersen et al (1997) found 9 blue profiles in 23 Class-0 sources, using the $J = 3 \rightarrow 2$ and $J = 4 \rightarrow 3$ lines of HCO$^+$ and H$^{13}$CO$^+$. After consideration of possible confusion by outflows etc, they identified six sources as good candidates for collapse. Mardones et al (1997) extended the search to Class-I sources with $T_{bol} < 200$ K, using CS and H$_2$CO lines. They introduced the line asymmetry as a collapse indicator:

$$\delta V = (V_{thick} - V_{thin})/\Delta V_{thin},$$

where $V_{thick}$ is the velocity of the peak of the opaque line, $V_{thin}$ is the velocity of the peak of the optically thin line, and $\Delta V_{thin}$ is the line width of the thin line. They confirmed many of the collapse candidates found by Gregersen et al (1997) and identified six more, but they found very few collapse candidates among the Class-I sources. The difference could be caused by using different tracers, because the CS and H$_2$CO lines are less opaque than the HCO$^+$ lines. To remove this uncertainty, Gregersen (1998) surveyed the Class-I sources of Mardones et al (1997) in HCO$^+$. Using $\delta V$ as the measure, the fraction of blue profiles did not decrease substantially between Class 0 and Class I. Most of these line profiles need further observations before they become bona fide candidates.

When does collapse begin? Surveys of the Class $-1$ cores might reveal very early stages of collapse. In the inside-out collapse picture, blue profiles should appear, if at all, only toward the center. In fact, blue profiles have been seen in a substantial number of these cores (Gregersen 1998, Lee et al 1999), and maps of one, L1544, show that the blue profiles are very extended spatially (Tafalla et al 1998). Clearly, extended blue profiles in Class $-1$ cores do not fit expectations for early collapse, and Tafalla et al argue that the velocities are higher than expected for ambipolar diffusion. If the regions producing the blue and red peaks are indeed approaching one another, they are forming a core more rapidly than in standard models, suggesting that some new ideas may be necessary (e.g. Nakano 1998, Myers & Lazarian 1998). For a current review of this field, see Myers et al (2000).

4.8 Summary of Isolated Star Formation

Distinct cores can be identified in tracers of dense ($n \geq 10^4$ cm$^{-3}$) gas; these cores are frequently associated with star formation. There is no clear evidence that they are magnetically subcritical, and some kinematic evidence suggests that the decay of turbulence, rather than ambipolar diffusion, is the critical feature.
An empirical evolutionary sequence, based on the spectral appearance of dust emission, and detailed theoretical models are now being tested by observations. The spatial distribution of dust emission is providing important tests by probing $n(r)$. Predictions of the evolution of spectral lines during collapse are available for the simplest theory, and observations of some sources match predictions of theory quite well. Evidence of collapse is now strong in a few cases, and surveys for distinctive line profiles have revealed many more possible cases.

5. CLUSTERED STAR FORMATION AND MASSIVE STARS

In this section, we address the issues of clustered formation, regardless of mass, and high-mass star formation, which seems to occur exclusively in clusters. In this review, the term cluster refers to a group of forming stars, regardless of whether the eventual outcome is a bound cluster. Since high-mass stars are rare, the nearest examples are more distant than is the case for low-mass-star formation. Together with the fact that they form in clusters, the greater distance makes it difficult to isolate individual events of star formation. On the other side of the balance, massive stars are more easily detectable at large distances because luminosity is such a strong function of mass. Heating of the surroundings makes them strong emitters in both dust and many spectral lines; the spectra of regions forming massive stars are often very rich, reflecting both a high excitation state and, in many cases, enhanced abundances, as complex chemistry is driven by elevated temperatures (van Dishoeck & Blake 1998). These features led early studies, when sensitivity was poor, to concentrate on regions forming massive stars. However, most of these advantages arise because the star is strongly influencing its surroundings; if we wish to know the preconditions, we will be misled. This problem is aggravated by the fast evolution of massive stars to the main sequence. Reviews of the topic of clustered star formation can be found in Elmegreen (1985), Lada & Lada (1991), and Lada (1999). Reviews focusing on the formation of massive stars include Churchwell (1993, 1999), Walmsley (1995), Stahler et al (2000), and Kurtz et al (2000).

5.1 Theoretical Issues

Some of the primary theoretical issues regarding the formation of massive stars have been reviewed by Stahler et al (2000). First, what is the relevant dividing line between low-mass and high-mass stars? For the star formation problem, the question is how far in mass the scenario for low-mass stars can be extended. Theoretically, the limit is probably about $10 \, M_\odot$, where stars reach the main sequence before the surrounding envelope is dissipated. Observations of the physical conditions in regions forming intermediate mass stars (Herbig Ae/Be stars and their more embedded precursors) can reveal whether modifications are needed at even lower masses. Because accretion through disks plays a crucial role in the standard
model, it is important to know the frequency and properties of disks around more massive stars.

Stars as massive as \(100 \, M_\odot\) seem to exist (Kudritzki et al 1992), but radiation pressure from the rapidly evolving stellar core should stop accretion before such masses can be built (e.g. Wolfire & Cassinelli 1987). In addition, massive stars produce very strong outflows (Shepherd & Churchwell 1996, Bachiller 1996). Because standard accretion theory cannot produce rates of mass accretion high enough to overwhelm these dispersive effects, some new effects must become important.

Related questions concern the formation of clusters. To what extent can the ideas of isolated core collapse be applied if there are competing centers of collapse nearby? If the collapse to form massive stars is supercritical, a whole region may collapse and fragment to form many stars.

The fact that the most massive stars are found near the centers of forming clusters has led to the suggestion that massive stars are built by collisional coalescence of stars or protostars (Bonnell et al 1997, 1998). This scheme requires high densities \((n_* \geq 10^4 \text{ stars pc}^{-3})\); for a mean stellar mass of \(1 \, M_\odot\), this corresponds to \(n \geq 2 \times 10^5 \text{ cm}^{-3}\). Even higher stellar densities are seen in the core of the Orion Nebula Cluster (Hillenbrand & Hartmann 1998).

The special problems of making the most massive stars are a subset of the larger question of explaining the mass distribution of all stars. There may be variations in the IMF between clusters (Scalo 1998), which can test theories. Hipparcos observations of nearby OB associations have extended the membership to lower-mass stars (de Zeeuw et al 1999), suggesting total masses of a few \(10^3 \, M_\odot\).

The main questions these issues raise for observations are whether the mass and density of cores are sufficient for forming clusters and massive stars and whether the mass distribution of clumps in a star-forming region can be related to the mass distribution of stars ultimately formed.

### 5.2 Overall Cloud and Core Properties

What do we know about the general properties of the galactic clouds? The broadest picture is provided by surveys of CO and \(^{13}\text{CO}\). Surveys of significant areas of the galaxy indicate that the power-law distribution in mass seen for small clouds \([dN(M) \propto M^{-\alpha}dM; \text{Section 3.1}]\) continues up to a cutoff at \(M \sim 6 \times 10^6 \, M_\odot\) (Williams & McKee 1997). Studies by Casoli et al (1984), Solomon & Rivolo (1989), and Brand & Wouterloot (1995) find \(1.4 \leq \alpha \leq 1.8\) over both inner and outer areas of the galaxy. Extinction surveys find flatter slopes (Scalo 1985), but Scalo & Lazarian (1996) suggest that cloud overlap affects the extinction surveys. The fact that \(\alpha < 2\) implies that most of the mass is in the largest structures, although there are issues of how to separate clouds at the largest scales. Because the star formation rate per unit mass, measured by CO, appears not to depend on cloud mass (Mead et al 1990, Evans 1991), the mass distribution supports the idea that most stars form in massive clouds (Elmegreen 1985). However, the enormous
spread (>10^2) in star formation rate per unit mass at any given mass, together with the fact that most of the molecular gas is sterile, suggests that comparisons to overall cloud masses, measured by CO, are not particularly relevant.

Surveys in molecular lines indicative of denser gas have generally been biased towards signposts of star formation. Exceptions are the CS J = 2 → 1 survey of L1630 (Lada et al 1991) and the CS J = 1 → 0 and J = 2 → 1 surveys of L1641 (Tatematsu et al 1993, 1998). These two clouds, also called Orion B and Orion A, are adjacent. In both cases, the CS J = 2 → 1 maps showed more contrast than maps of 13CO (Bally et al 1987), with CS J = 1 → 0 being somewhat intermediate. Maps of higher-J transitions have been less complete, but show still less area covered by emission. The CS surveys detected <20% of the total mass in both clouds (Lada et al 1991; Tatematsu, personal communication). The J = 2 → 1 emission in L1641 is somewhat smoother than the J = 2 → 1 emission from L1630 (Tatematsu et al 1998), and this difference may be reflected in the distribution of star formation. Star formation in L1641 appears to include a distributed component (Strom et al 1993); in contrast, star formation in L1630 is tightly concentrated in clusters associated with massive cores of dense gas (Lada 1992, Li et al 1997).

Excitation analysis of CS lines with higher critical density in L1630 shows that the star-forming regions all contain gas with n ≥ 10^5 cm^-3 (Lada et al 1997). These results suggest that surveys in lines of high n_c(jk) are relevant for characterizing star formation regions. Of the possible tracers, CS (e.g. Tatematsu et al 1993) and NH_3 (e.g. Harju et al 1993) have been most widely surveyed. In comparison to cores in Taurus, where only low-mass stars are forming, cores in the Orion clouds tend to be more massive and to have larger line widths when observed with the same tracer. The differences are factors of 2–4 for the majority of the cores, but larger for the cores near the Orion Nebula and those forming clusters in L1630 (Lada et al 1991).

CS transitions have been surveyed toward ultracompact (UC) HII regions, H_2O masers, or luminous IRAS sources (see Kurtz et al 2000). Since the IRAS survey became available, most samples are drawn from the IRAS catalog with various color selection criteria applied. The most complete survey (Bronfman et al 1996) was toward IRAS sources with colors characteristic of UC HII regions (Wood & Churchwell 1989) over the entire galactic plane. Bronfman et al found CS J = 2 → 1 emission (see Table 1 for density sensitivity) in 59% of 1427 IRAS sources, and the undetected sources were either weak in the far-infrared or had peculiar colors. Searches toward H_2O masers have used the catalogs of Braz & Epchtein (1983) and Cesaroni et al (1988). Surveys of CS J = 2 → 1 (Zinchenko et al 1995, Juvela 1996) toward southern H_2O masers found detection rates of ~100%, suggesting that dense, thermally excited gas surrounds the compact, ultradense regions needed to produce H_2O masers. The detection rate drops in higher-J transitions of CS (Plume et al 1992, 1997) but is still 58% in the CS J = 7 → 6 line, which probes higher densities (Table 1). An LVG, multitransition study of CS lines found
\langle \log n (\text{cm}^{-3}) \rangle = 5.9 \text{ for 71 sources and a similar result from a smaller sample using C}^{34}\text{S data (Plume et al 1997). Densities derived assuming LVG fall between the average and maximum densities in clumpy models with a range of densities (Juvela 1997, 1998).}

Maps of the cores provide size and mass information. Based on the sizes and masses of 28 cores mapped in the CS $J = 2 \rightarrow 1$ line (Juvela 1996), one can compute a mean size, $\langle l \rangle = 1.2 \pm 0.5 \text{ pc}$; mean virial mass, $\langle M_V \rangle \sim 5500 \text{ M}_\odot$; and $\langle M_N \rangle \sim 4900 \text{ M}_\odot$. Although the two mass estimates agree on average, there can be large differences in individual cases. Remarkably, cloud structure does not introduce a big uncertainty into the cloud masses; using a clumpy cloud model, (see Section 5.4), Juvela (1998) found that $M_N$ increased by a factor of 2 on average compared with homogeneous models and agreed with $M_V$ to within a factor of 2. Plume et al (1997) obtained similar results from strip maps of CS $J = 5 \rightarrow 4$: $\langle l \rangle = 1.0 \pm 0.7 \text{ pc (average over 25 cores); } \langle M_V \rangle = 3800 \text{ M}_\odot$ (16 cores). As usual mean values must be regarded with caution; there is a size distribution. As cores with weaker emission are mapped, the mean size decreases; an average of 30 cores with full maps of $J = 5 \rightarrow 4$ emission gives $\langle l \rangle = 0.74 \pm 0.56 \text{ pc}$, with a range of 0.2–2.8 pc (Y Shirley, unpublished results).

Churchwell et al (1992) surveyed 11 UC HII regions for CS $J = 2 \rightarrow 1$ and $J = 5 \rightarrow 4$ emission, leading to estimates of $n \geq 10^5 \text{ cm}^{-3}$. Cesaroni et al (1991) surveyed 8 UC HII in three transitions of CS and C$^{34}$S and estimated typical sizes of 0.4 pc, masses of 2000 M$_\odot$, and densities of $10^6 \text{ cm}^{-3}$. More extensive surveys have been made in NH$_3$; Churchwell et al (1990) found NH$_3$ $(J, K) = (1, 1)$ and (2,2) emission from 70% of a sample of 84 UC HII regions and IRAS sources with similar colors. They derived $T_K$, finding a peak in the distribution around 20 K, but a significant tail to higher values. Further studies in the (4,4) and (5,5) lines toward 16 UC HII regions with strong (2,2) emission (Cesaroni et al 1992) detected a high fraction. Estimates for $T_K$ ranged from 64 to 136 K and sizes of 0.5 pc. Two sources indicated much higher densities and NH$_3$ abundances. Follow-up studies with the VLA (Cesaroni et al 1994a, 1998) revealed small ($\sim 0.1$ pc), hot ($T_K \sim 50–200$ K), dense ($n = 10^7 \text{ cm}^{-3}$) regions with enhanced NH$_3$ abundances. These hot cores (discussed below) are slightly displaced from the UC HII, but coincide with H$_2$O masers.

Magnetic-field strengths have been measured with the Zeeman effect toward about 10 regions of massive-star formation. The fields are substantially stronger than the fields seen in isolated, low-mass cores, but the masses are also much higher. In most cases the mass-to-flux ratio is comparable to the critical ratio, once geometrical effects are considered (Crutcher 1999b). Given the uncertainties and sample size, it is too early to decide whether regions forming massive stars are more likely to be supercritical than regions forming only low-mass stars.

The ionization fraction in the somewhat more massive Orion cores appears to be very similar to that in low-mass cores: $-6.9 < \log x_e < -7.3$ (Bergin et al 1999). The most massive cores in their sample have $x_e \leq 10^{-8}$, as do some
of the massive cores studied by de Boisanger et al (1996). Expressed in terms of column density, the decline in $x_e$ appears around $N \sim 3 \times 10^{22}$ cm$^{-2}$. At $x_e = 10^{-8}$, $t_{AD} = 7 \times 10^3$ years, $\sim 0.1 t_{AD}$ in isolated, low-mass cores. Even if the massive cores are subcritical, their evolution should be faster than that of low-mass cores.

To summarize, the existing surveys show ample evidence that massive star formation usually takes place in massive ($M > 10^3 M_\odot$), dense ($n \sim 10^6$ cm$^{-3}$) cores, consistent with the requirements inferred from the study of young clusters and associations, and with conditions needed to form the most massive stars by mergers. Cores with measured $B_z$ seem to be near the boundary between subcritical and supercritical cores.

5.3 Evolutionary Scenarios and Detailed Theories

To what extent can an evolutionary scenario analogous to the class system be constructed for massive-star formation? Explicit attempts to fit massive cores into the class system have relied on surveys of IRAS sources. Candidates for massive Class-0 objects, with $L > 10^3 L_\odot$, have been found (Wilner et al 1995, Molinari et al 1998). One difficulty with using the shape of the spectral energy distribution for massive-star formation is that dense, obscuring material usually surrounds objects even after they have formed, and a single star may be quite evolved but still have enough dust in the vicinity to have the same spectral energy distribution as a much younger object. The basic problem is the difficulty in isolating single objects. Also, the role of disks in massive regions is less clear, and they are unlikely to dominate the spectrum, as they do in low-mass Class-II sources. Other markers, such as the detection of radio continuum emission, must be used as age indicators. Hot cores provide obvious candidates to be precursors of UC HII regions, but some have embedded UC HII regions and may be transitional (Kurtz et al 2000). The chemical state of massive cores may also provide an evolutionary sequence; Helmich et al (1994) suggested an evolutionary ordering of three sources in the W3 region based on their molecular spectra and chemical models (see van Dishoeck & Blake 1998).

Although theories for clustered- and massive-star formation are much less developed, some steps have been taken (e.g. Bonnell et al 1998, Myers 1998). The larger $\Delta v$ in regions forming massive stars imply that turbulence must be incorpo-
rated into the models. Myers & Fuller (1992) suggested a “thermal-non-thermal” (TNT) model, in which $n(r)$ is represented by the sum of two power laws and the term with $p = 1$ dominates outside the radius ($r_{TNT}$) at which turbulent motions dominate thermal motions. McLaughlin & Pudritz (1997) develop the theory of a logatropic sphere, which has a density distribution approximated by $p = 1$. Collapse in such a configuration leads to power laws in the collapsing region with similar form to those in the collapsing isothermal sphere, but with higher densities and lower velocities. These ideas lead to accretion rates that increase with time and timescales for forming massive stars that are much weaker functions of the
final stellar mass than is the case for the isothermal sphere (Section 4.5). Recent
simulations of unmagnetized fragmentation that follow the interaction of clumps
find that the mass spectrum of fragments steepens from $\alpha = 1.5$ to a lognormal
distribution of the objects likely to form stars (e.g. Klessen et al 1998). To avoid an
excessive global star formation rate (Section 2) and distortion of the clump mass
spectrum in the bulk of the cloud, this process must be confined to star-forming
regions in clouds.

5.4 Filaments, Clumps, Gradients, and Disks

An important issue is whether the dense cores have overall density gradients or
internal structures (clumps) that are likely to form individual stars and whether the
mass distribution is like that of stars. Unfortunately, the terms “clumps” and “cores”
have no standard usage; I generally use “cores” to refer to regions that appear in
maps of high-excitation lines and “clumps” to mean structures inside cores, except
where a different usage is well established (e.g. “hot cores”). Myers (1998) has
suggested the term “kernels” to describe clumps within cores. Cores themselves
are usually embedded in structures traced by lines with lower critical density, and
these are also called clumps by those who map in these lines. Many of these low-
density structures are quite filamentary in appearance; examples include the $^{13}$CO
maps of L1641 (Orion B) of Bally et al (1987). In some cases, this filamentary
structure is seen on smaller scales in tracers of high density or column density
(Figure 2; e.g. Johnstone & Bally 1999).

The clumpy structure of molecular clouds measured in low-excitation lines
suggests that dense cores will be clumpy as well. Suggestions of clumpy structure
came from early work comparing densities derived from excitation analysis in
different tracers, but smooth density gradients provided an alternative (e.g. Evans
1980). Multitransition studies of three cores in CS (Snell et al 1984), C$^{34}$S (Mundy
et al 1986), and H$_2$CO (Mundy et al 1987) found no evidence for overall density
gradients; the same high densities were derived over the face of the core, while
the strength of the emission varied substantially. This was explained in a clumpy
model with clump-filling factors of the dense gas $f_c \sim 0.03–0.3$, based on a
comparison of $M_V$ with $M_n$ (Snell et al 1984). This comparison forms the basis
for most claims of unresolved clumps.

Observations at higher resolution support the idea of clumps postulated by Snell
et al (1984). For example, Stutzki & Güsten (1990) deconvolved 179 clumps from
a map of C$^{18}$O $J = 2 \rightarrow 1$ emission near M17. Because of overlap, far fewer
clumps are apparent to the eye; assumptions about the clump shape and structure
may affect the deconvolution. Maps of the same source in several CS and C$^{34}$S
lines (Wang et al 1993) could be reproduced with the clump catalog of Stutzki &
Güsten, but only with densities about 5 times higher than they found. Thus the
clumps themselves must have structure, either a continuation of clumpiness or
smooth gradients. Because the inferred clumps are now similar in size to the cores
forming low-mass stars, a natural question is whether massive cores are fragmented
into many clumps which can be modeled as if they were isolated cores. In favor of this view, Stutzki & Güsten (1990) noted that the Jeans length was similar to the size of their clumps.

A significant constraint on this picture is provided by the close confinement of the clumps; unlike the picture of isolated-core formation, the sphere of influence of each clump will be limited by its neighbors. A striking example is provided by the dust continuum maps of the ρ Ophiuchi cloud (Figure 1), our nearest example of cluster formation, albeit with no very massive stars. Within about six cores of size 0.2 pc, Motte et al (1998) find about 100 structures with sizes of 1000–4000 AU. They deduce a fragmentation scale of 6000 AU, five times smaller than isolated cores in Taurus. Thus the “feeding zone” of an individual clump is considerably less, and the evolution must be more dynamic, with frequent clump-clump interactions, than is the case for isolated-star formation. This picture probably applies even more strongly to the more massive cores. In ρ Ophiuchi, the clump mass spectrum above 0.5 M⊙ steepens to α = 2.5, close to the value for stars (Motte et al 1998), in agreement with predictions of Klessen et al (1998). A similar result (α = 2.1) is found in Serpens, using millimeter interferometry (Testi & Sargent 1998). Although more such studies are needed, these results suggest that dust continuum maps do trace structures that are likely precursors of stars, opening the study of the origin of the IMF to direct observational study.

Some of the less massive, relatively isolated cores, such as NGC2071, S140, and GL2591, have been modeled with smooth density and temperature gradients (Zhou et al 1991, 1994b; Carr et al 1995; van der Tak et al 1999). Models with gradients can match the relative strengths of a range of transitions with different excitation requirements, improving on homogeneous models. Zhou et al (1994) summarized attempts to deduce gradients and found preliminary evidence that, as core mass increases, the tendency is first toward smaller values of p. The most massive cores showed little evidence for any overall gradient and more tendency toward clumpy substructure. This trend needs further testing, but it is sensible if more massive cores form clusters. Lada et al (1997) found that the L1630 cores forming rich embedded clusters with high efficiency tended to have larger masses of dense (n > 10^5 cm⁻³) gas, but a lower volume filling factor of such gas, indicating more fragmentation.

However, the line profiles of optically thick lines predicted by models with gradients are usually self-absorbed, while the observations rarely show this feature in massive cores. Clumps within the overall gradients are a likely solution. The current state of the art in modeling line profiles in massive cores is the work of Juvela (1997, 1998), who has constructed clumpy clouds from both structure tree and fractal models, performed three-dimensional radiative transport and excitation, and compared the model line profiles to observations of multiple CS and C³⁴S transitions in massive cores. He finds that the clumpy models match the line profiles much better than nonclumpy models, especially if macroturbulence dominates microturbulence. Structure trees (Houlahan & Scalo 1992) match the data better than fractal models, but overall density and/or temperature gradients with p + q ≈ 2 are needed in addition to clumps.
The study of gradients versus clumps in regions forming intermediate-mass stars could help to determine whether conditions change qualitatively for star formation above some particular mass and how this change is related to the outcome. Using near-infrared observations of regions with Herbig Ae/Be stars, Testi et al (1997) found that the cluster mode of star formation becomes dominant when the most massive star has a spectral type earlier than B7. Studies of the far-infrared emission from dust remaining in envelopes around Herbig Ae/Be stars found values of $\rho$ ranging from 0.5 to 2 (Natta et al 1993). Maps of dust continuum emission illustrate the difficulties—the emission may not peak on the visible star, but on nearby, more embedded objects (Henning et al 1998, Di Francesco et al 1998). Detailed models of several suitable sources yield $\rho = 0.75$ to 1.5 (Henning et al 1998, Colomé et al 1996). Further work is needed to determine whether a change in physical conditions can be tied to the change to cluster mode.

Many Herbig Ae stars have direct evidence for disks from interferometric studies of dust emission (Mannings & Sargent 1997), although fewer Herbig Be stars have such direct evidence (Di Francesco et al 1997). For a review, see Natta et al (2000). Disks may be more common during more embedded phases of B star formation; Shepherd & Kurtz (1999) have found a large (1000-AU) disk around an embedded B2 star. The statistics of UC HII regions may provide indirect evidence for disks around more massive stars. Because such regions should expand rapidly unless confined, the large number of such regions posed a puzzle (Wood & Churchwell 1989). Photoevaporating disks have been suggested as a solution (Hollenbach et al 1994). Such disks have also been used to explain very broad recombination lines (Jaffe & Martín-Pintado 1999). Kinematic evidence for disks will be discussed in Section 5.5.

A particular group of clumps (or cores) deserves special mention, hot cores (e.g. Ohishi 1997). First identified in the Orion cloud (Genzel & Stutzki 1989), ~20 are now known (see Kurtz et al 2000). They are small regions ($l \sim 0.1$ pc), characterized by $T_K > 100$ K, $n > 10^7$ cm$^{-3}$, and rich spectra, probably reflecting enhanced abundances, as well as high excitation (van Dishoeck & Blake 1998). Theoretical issues have been reviewed by Millar (1997) and Kaufman et al (1998), who argue that hot cores are likely to be heated internally, but they often lack radio continuum emission. Because dynamical timescales for gas at such densities are short, these may plausibly be precursors to the UC HII regions.

The evidence for flatter density distribution in regions of intermediate mass supports the relevance of models like the TNT or logatropic sphere models in massive regions (Section 5.3), but it will be important to study this trend with the same methods now being applied to regions forming low-mass stars, with due regard for the greater distance to most regions forming massive stars. The increasingly fragmented structure in more massive cores and the increased frequency of clusters above a certain mass are consistent with a switch to a qualitatively different mode of star formation, for which different theories are needed. Finally, the common appearance of filaments may support a continuing role for turbulence in dense regions, because simulations of turbulence often produce filamentary structures (e.g. Scalo et al 1998).
5.5 Kinematics

Lada et al (1991) found only a weak correlation between line width and size, disappearing entirely for a different clump definition, in the L1630 cores (Goodman Type-2 relation, see Section 4.3). Caselli & Myers (1995) also found that the Type-1 line width-size relation (with only nonthermal motions included, $\Delta v_{NT} \propto R'$) is flatter in massive cloud cores ($\gamma = 0.21 \pm 0.03$) than in low-mass cores ($\gamma = 0.53 \pm 0.07$); in addition, the correlation is poor (correlation coefficient of 0.56) although the correlation is better for individual cores (Type-3 relations). Caselli & Myers (1995) also noted that nonthermal (turbulent) motions are much more dominant in more massive cores and find good agreement with predictions of the TNT model. The “massive” cores in the Caselli & Myers study are mostly the cores in Orion with masses between 10 and 100 M☉. The much more massive ($\langle M_V \rangle = 3800$ M☉) cores studied by Plume et al (1997) exhibit no statistically significant line width-size relation at all (correlation coefficient is 0.26) and the line widths are systematically higher (by factors of 4–5) for a given size than would be predicted by the relationships derived for low- and intermediate-mass cores (Caselli & Myers 1995). In addition, the densities of these cores exceed by factors of 100 the predictions of density-size relations found for less massive cores (Myers 1985). The regions forming truly massive stars are much more dynamic, as well as much denser, than would be expected from scaling relations found in less massive regions. The typical line width in massive cores is 6–8 km s⁻¹, corresponding to a one-dimensional velocity dispersion of 2.5–3.4 km s⁻¹, similar to that of the stars in the Orion Nebula Cluster (Hillenbrand & Hartmann 1998). Larson (1981) noted that regions of massive-star formation, like Orion and M17, did not follow his original line width-size relation, suggesting that gravitational contraction would decrease size while keeping $\Delta v$ roughly constant or increasing it.

Searching for collapse in massive cores is complicated by the turbulent, clumpy structure, with many possible centers of collapse, outflow, etc. A collapse signature may indicate an overall collapse of the core, with accompanying fragmentation. In fact, self-absorbed line profiles from regions forming massive stars are rather rare (Plume et al 1997). A possible collapse signature has been seen in CS emission toward NGC 2264 IRS, a Class-I source with $L \sim 2000$ L☉ (Wolf-Chase & Gregersen 1997). If an HII region lies at the center of a collapsing core, absorption lines should trace only the gas in front and should be redshifted relative to the emission lines. Failure to see this effect, comparing H2CO absorption to CO emission, supported an early argument against the idea that all clouds were collapsing (Zuckerman & Evans 1974). A more recent application of this technique to dense cores, using high-excitation lines of NH₃, showed no preference for red-shifted absorption (Olmi et al 1993) overall, but a few dense cores do show this kind of effect. These sources include W49 (Welch et al 1988, Dickel & Auer 1994), G10.6–0.4 (Keto et al 1988), and W51 (Zhang & Ho 1997, Zhang et al 1998a).

Dickel & Auer (1994) tested different collapse scenarios against observations of HCO⁺ and favored free-fall collapse, with $n \propto r^{-1.5}$ and $v \propto r^{-0.5}$ throughout
they noted that more complex motions are present on small scales. Keto et al (1988) used NH₃ observations with 0.3'' resolution to separate infall from rotational motions toward the UC HII region, G10.6–0.4. Zhang & Ho (1997) used NH₃ absorption and Zhang et al (1998a) added CS J = 3 → 2 and CH₃CN observations to identify collapse onto two UC HII regions, W51e2 and W51e8, inferring infall velocities of about 3.5 km s⁻¹ on scales of 0.06 pc. Young et al (1998) have tested various collapse models against the data on W51e2 and favor a nearly constant collapse velocity (v ~ 5 km s⁻¹) and n(r) ~ r⁻². Mass infall rates of about 6 × 10⁻³ (Zhang et al 1998a) to 5 × 10⁻² (Young et al 1998) M☉ year⁻¹ were inferred for W51e2. Similar results were found in G10.6–0.4 (Keto et al 1988), and even more extreme mass infall rates (10⁻² to 1 M☉ year⁻¹) have been suggested for W49A, a distant source with enormous mass (~10⁶ M☉) and luminosity (L ~ 10⁷ L☉) (Welch et al 1988). These high infall rates may facilitate formation of very massive stars (Section 5.1) and help confine UC HII regions (Walmsley 1995).

Large transverse velocity gradients have been seen in some hot cores, including G10.6–0.4 (Keto et al 1988), W51 (Zhang & Ho 1997), and IRAS20126 + 4104 (Cesaroni et al 1997, Zhang et al 1998b). For example, gradients reach 80 km s⁻¹ pc⁻¹ in the NH₃ (J, K) = (4, 4) line and 400 km s⁻¹ pc⁻¹ in the CH₃CN J = 6 → 5 line toward G29.96−0.02 and G31.41+0.31 (Cesaroni et al 1994b, 1998). Cesaroni et al (1998) interpret the gradients in terms of rotating disks extending to about 10⁴ AU. By using the dust continuum emission at 3 mm, they deduce disk masses up to 4200 M☉ for G31.41+0.31.

5.6 Implications for Larger Scales

Since most stars form in the massive cores discussed in this section (Elmegreen 1985), they are most relevant to issues of star formation on a galactic scale. If the luminosity is used to trace star formation rate (e.g. Rowan-Robinson et al 1997, Kennicutt 1998), the star formation rate per unit mass is proportional to L/M. Considering clouds as a whole, ⟨L/M⟩ ~ 4 in solar units (e.g. Mooney & Solomon 1988), with a spread exceeding a factor of 10² (Evans 1991). Using CS J = 5 → 4 emission to measure M in the dense cores, Plume et al (1997) found ⟨L/M⟩ = 190 with a spread of a factor of 15. The star formation rate per unit mass is much higher and less variable if one avoids confusion by the sterile gas. The average L/M seen in dense cores in our Galaxy is similar to the highest value seen in luminous infrared galaxies, where M is measured by CO (Sanders et al 1991, Sanders & Mirabel 1998). The most dramatic starburst galaxies behave as if their entire interstellar medium has conditions like those in the most active, massive dense cores in our Galaxy. Some studies (e.g. Mauersberger & Henkel 1989) indeed found strongly enhanced CS J = 5 → 4 emission from starburst galaxies. It will be interesting to observe high-J CS lines in the most luminous galaxies to compare to the conditions in massive cores in our Galaxy. Perhaps the large scatter in L/M seen in galaxies will be reduced if CS, rather than CO, is
used as a measure of the gas, ultimately leading to a better understanding of what controls galactic star formation rates (see Kennicutt 1998).

5.7 Summary of Clustered Star Formation

The cloud mass distribution found for lower-mass objects continues to massive clouds, but less is known about the distribution for dense cores. Very massive cores clearly exist, with sufficient mass \( M > 10^3 M_\odot \) to make the most massive clusters and associations. These cores are denser and much more dynamic than cores involved in isolated-star formation, with typical \( n \sim 10^6 \) cm\(^{-3}\) and line widths about 4–5 times larger than predicted from the line width-size relation. Pressures in massive cores (both thermal and turbulent) are substantially higher than in lower-mass cores. The densities match those needed to form the densest clusters and the most massive stars by coalescence. There are some cores with evidence of overall collapse, but most do not show a clear pattern. There is some evidence that more massive regions have flatter density profiles and that fragmentation increases with mass, but more studies are needed. High-resolution studies of nearby regions of cluster formation are finding many clumps, limiting the feeding zone of a particular star-forming event to \( l \sim 6000 \) AU, much smaller than the reservoirs available in the isolated mode. In some cases, the clump mass distribution approaches the slope of the IMF, suggesting that the units of star formation have been identified. Studies of intermediate-mass stars indicate that a transition to clustered mode occurs at least by a spectral type of B7.

6. CONCLUSIONS AND FUTURE PROSPECTS

The probes of physical conditions have been developed and are now fairly well understood. Some physical conditions have been hard to measure, such as the magnetic-field strength, or hard to understand, notably the kinematics. Star-forming structures or cores within primarily sterile molecular clouds can be identified by thresholds in column density or density. Stars form in distinct modes, isolated and clustered, with massive stars forming almost exclusively in a clustered mode. The limited number of measurements of magnetic field leave open the question of whether cores are subcritical or supercritical and whether this differs between the isolated and clustered mode. Cores involved in isolated-star formation may be distinguished from their surroundings by a decrease in turbulence to subsonic levels, but clustered-star formation occurs in regions of enhanced turbulence and higher density, compared with isolated star formation.

Evolutionary scenarios and detailed theories exist for the isolated mode. The theories assume cores with extended, power-law density gradients, leading to the mass accretion rate as the fundamental parameter. Detailed tests of these ideas are providing overall support for the picture, but also raising questions about the detailed models. Notably, kinematic evidence of gravitational collapse has finally
been identified in a few cases. The roles of turbulence, the magnetic field, and rotation must be understood, and the factors that bifurcate the process into single- or multiple-star formation must be identified. Prospects for the future include a less biased census for cores in early stages and improved information on density gradients, both facilitated by the appearance of cameras at millimeter and submillimeter wavelengths on large telescopes. Antenna arrays operating at these wavelengths will provide more detailed information on the transition region between envelope and disk and will be used to study early disk evolution and binary fraction. Future, larger antenna arrays will probe disk structure to scales of a few AU. Finally, a closer coupling of physical and chemical studies with theoretical models will provide more pointed tests of theory.

Theories and evolutionary scenarios are less developed for the clustered mode, and our understanding of the transition between isolated and clustered mode is still primitive. Current knowledge suggests that more massive cores have flatter density distributions and a greater tendency to show substructure. At some point, the substructure dominates, and multiple centers of collapse develop. With restricted feeding zones, the mass accretion rate gives way to the mass of clump as the controlling parameter, and some studies of clump mass spectra suggest that the stellar IMF is emerging in the clump mass distribution. The most massive stars form in very turbulent regions of very high density. The masses and densities are sufficient to form the most massive clusters and to explain the high stellar density at the centers of young clusters. They are also high enough to match the needs of coalescence theories for the formation of the most massive stars. As with isolated regions, more and better measurements of magnetic fields are needed, along with a less biased census, particularly for cool cores that might represent earlier stages. Larger antenna arrays will be able to separate clumps in distant cores and determine mass distributions for comparison with the IMF. Larger airborne telescopes will provide complementary information on luminosity sources in crowded regions. Observations with high spatial resolution and sensitivity in the mid-infrared will provide clearer pictures of the deeply embedded populations, and mid-infrared spectroscopy with high spectral resolution could trace kinematics close to the forming star. Deeper understanding of clustered star formation in our Galaxy will provide a foundation for understanding the origin and evolution of galaxies.

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